



Modeling of clouds in the Earth

Atmosphere:

Turbulence, Convection & Cold Pools

Exoplanet-bacteria-mars Meeting, 10.7.2020

BETTINA MEYER

With Thanks to: Jan Haerter (NBI)

1. MOTIVATION

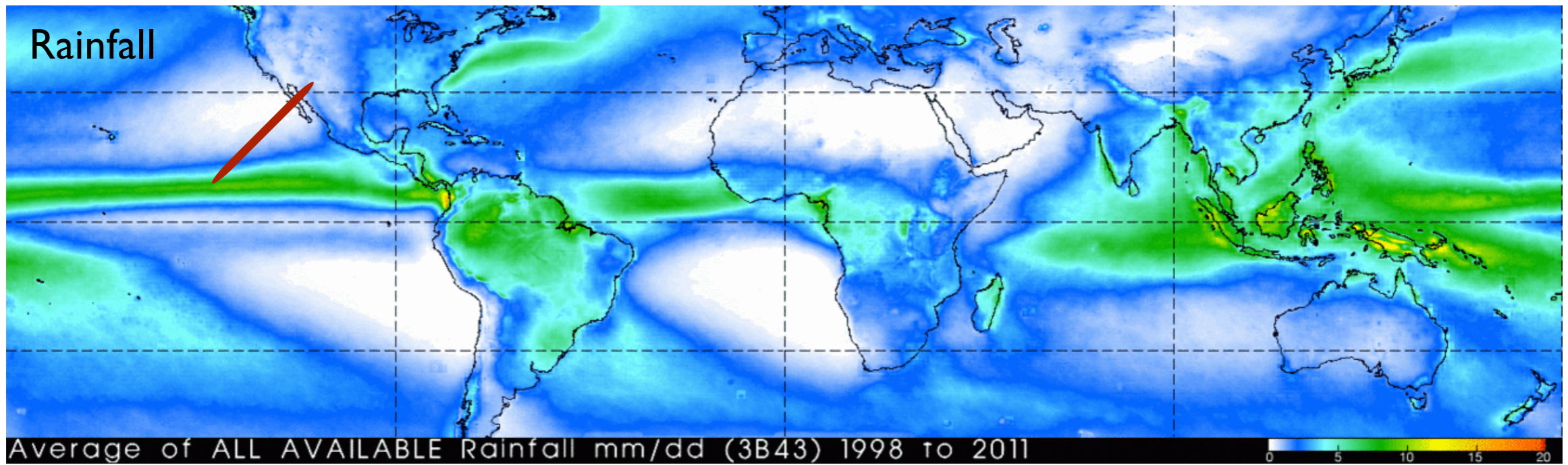


Figure: mean precipitation from TRMM satellite observations (wikipedia.org)

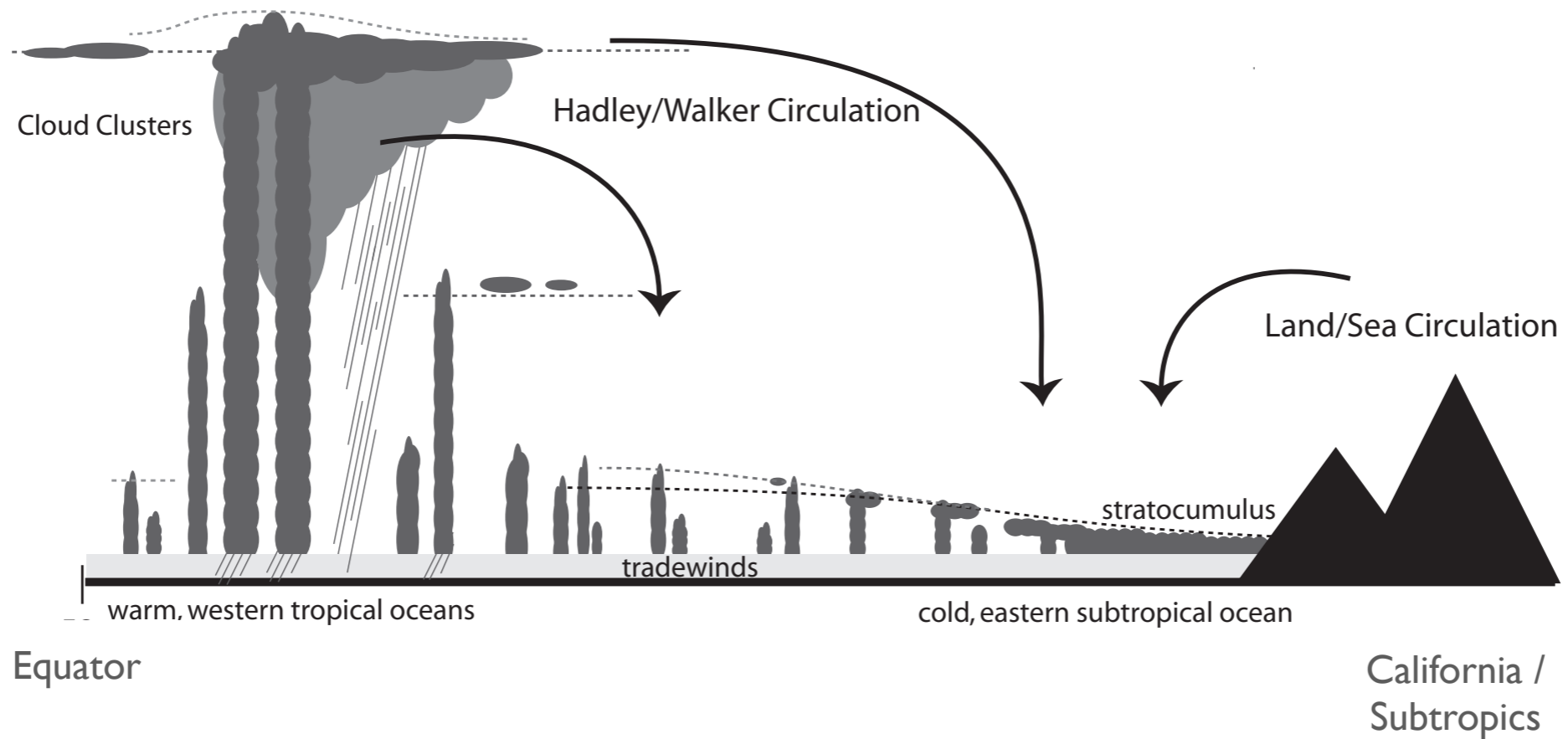


Figure: Atmospheric Moist Convection, B. Stevens (2005)

Deep Convection



Shallow Convection



Stratocumulus

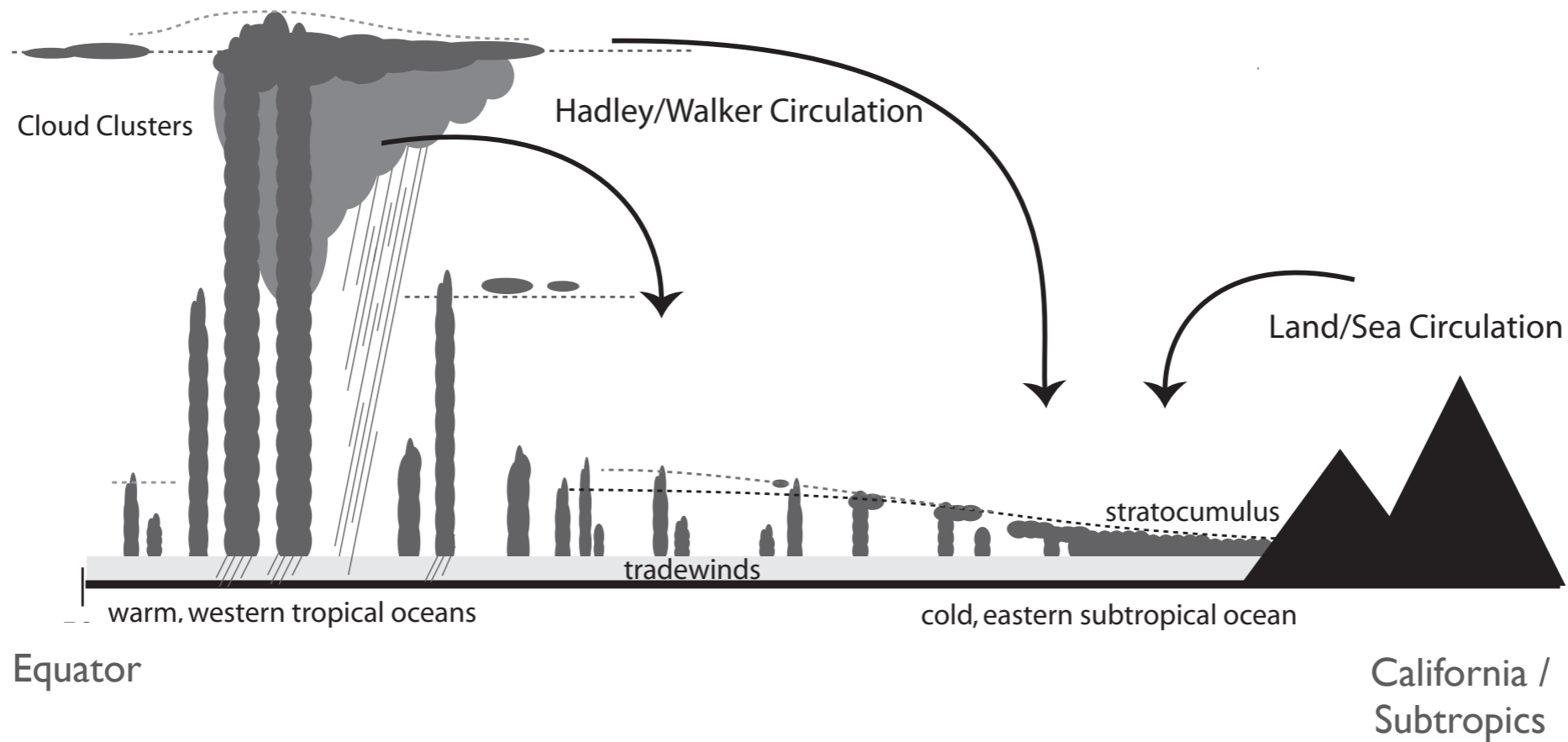
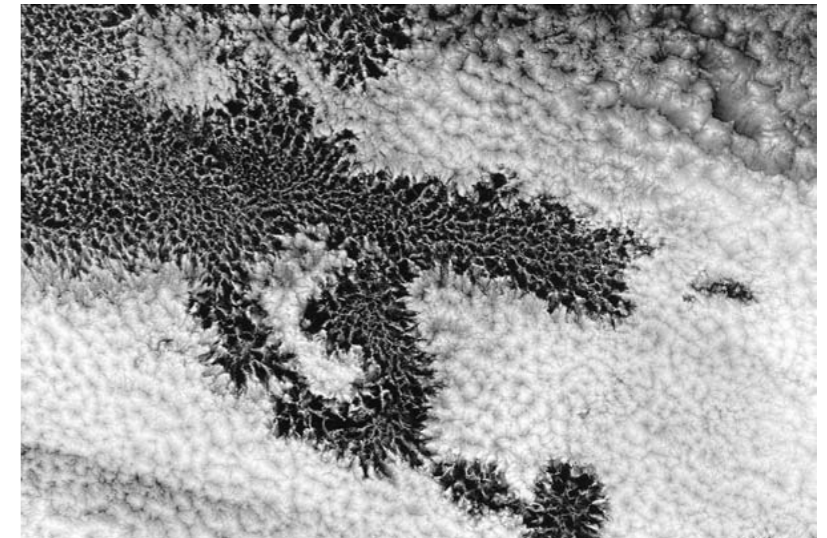


Figure: Atmospheric Moist Convection, B. Stevens (2005)

Climate & Weather Models

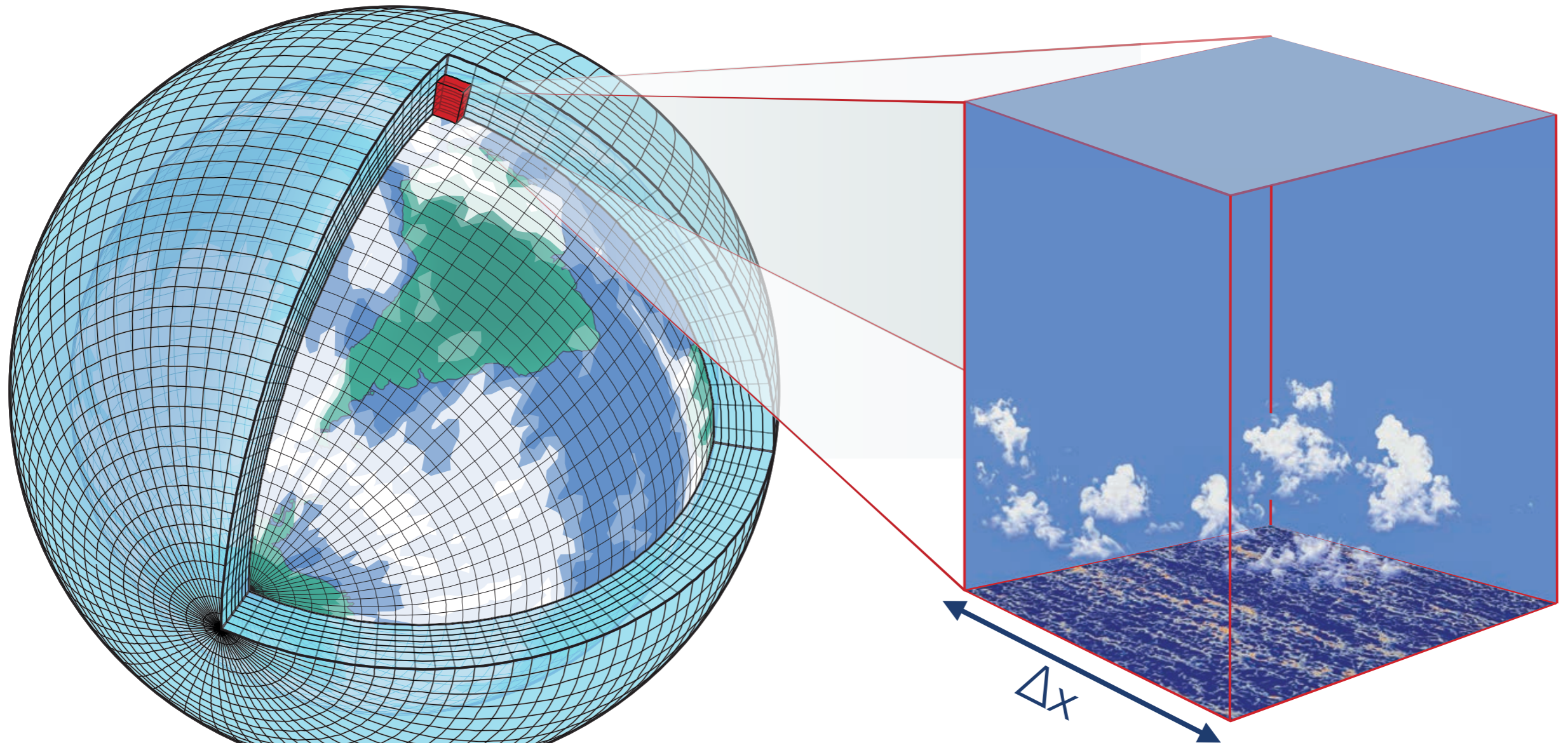


Figure: Schneider et al., 2017

grid resolution weather models:

- global: $\Delta x \sim O(10\text{km})$
- regional: $\Delta x \sim O(1\text{km})$

grid resolution climate models: $\Delta x \sim O(50-100\text{km})$

High-Resolution Modeling (Large-Eddy-Simulation)

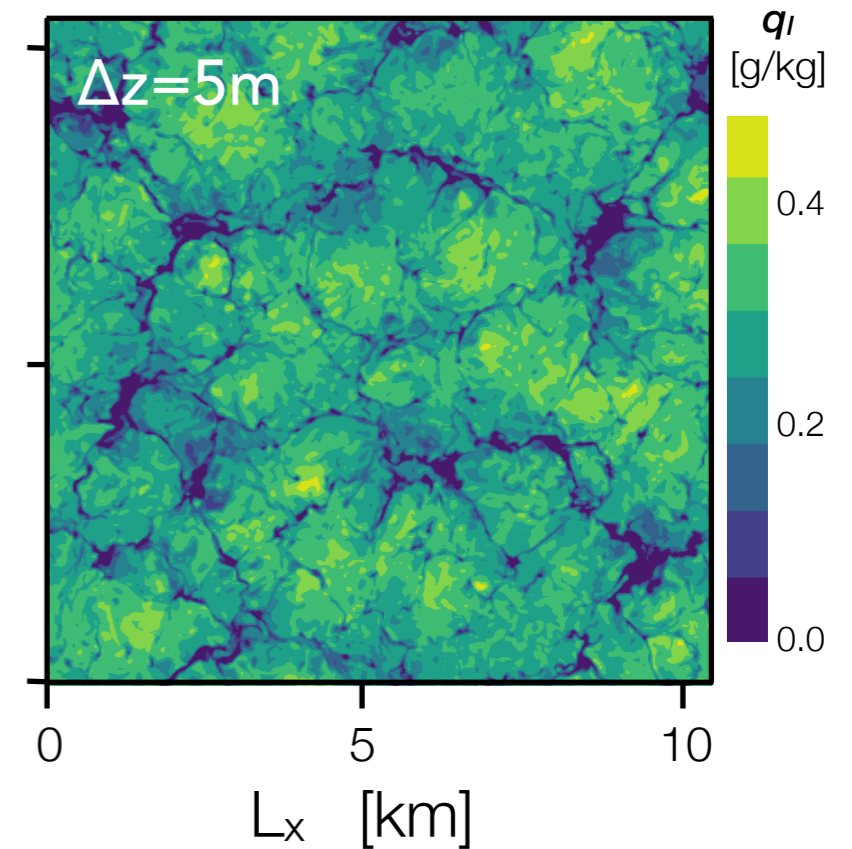
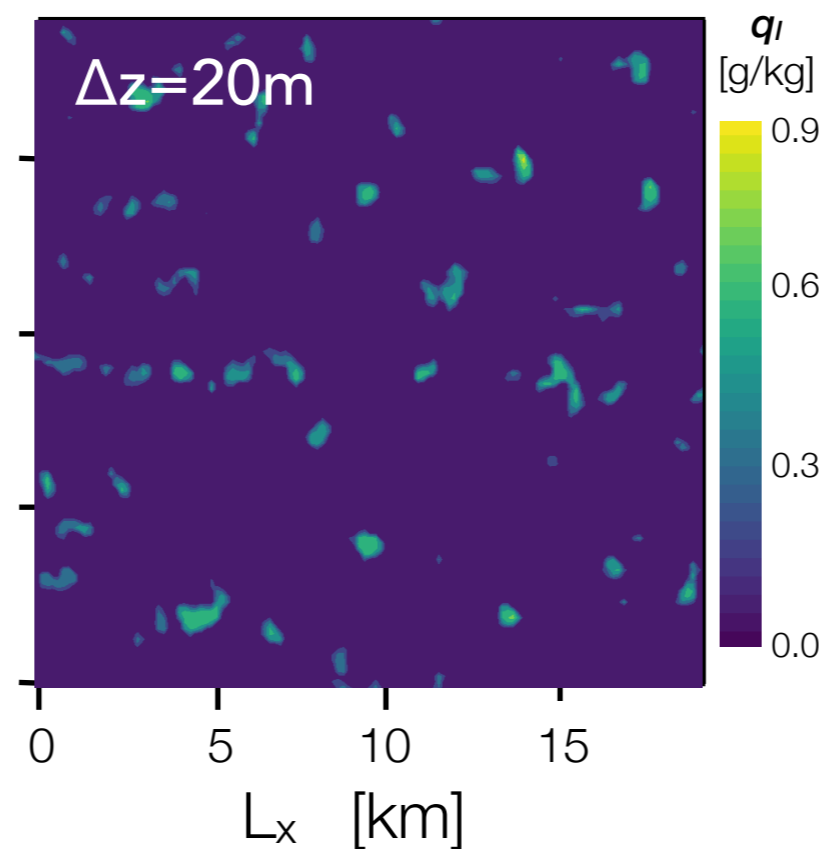
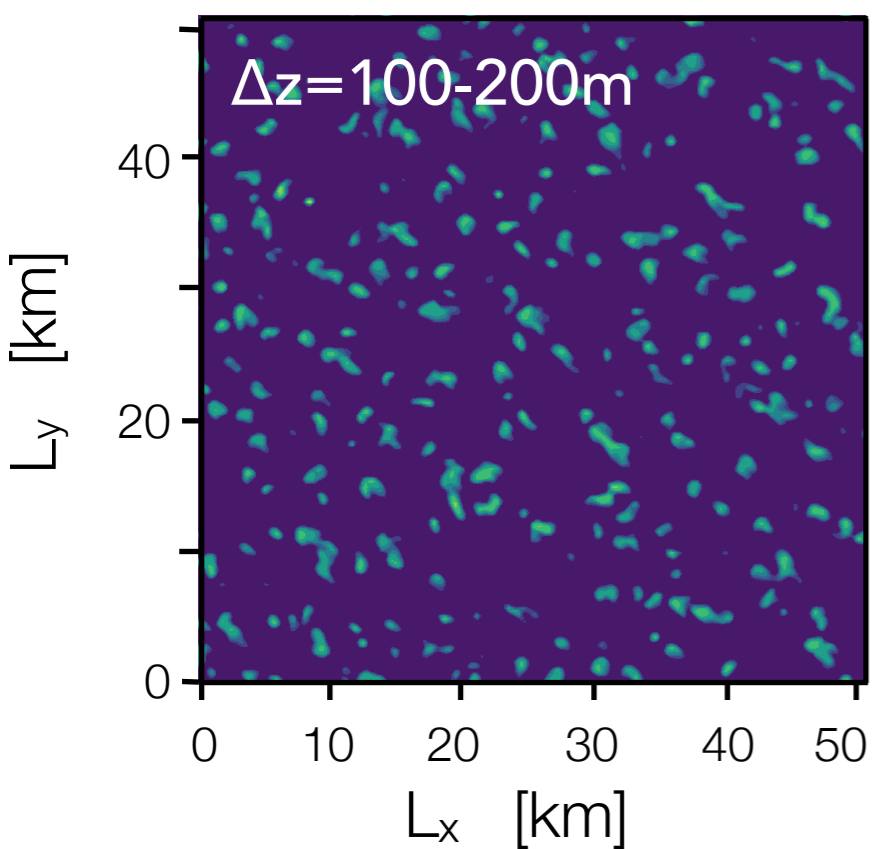
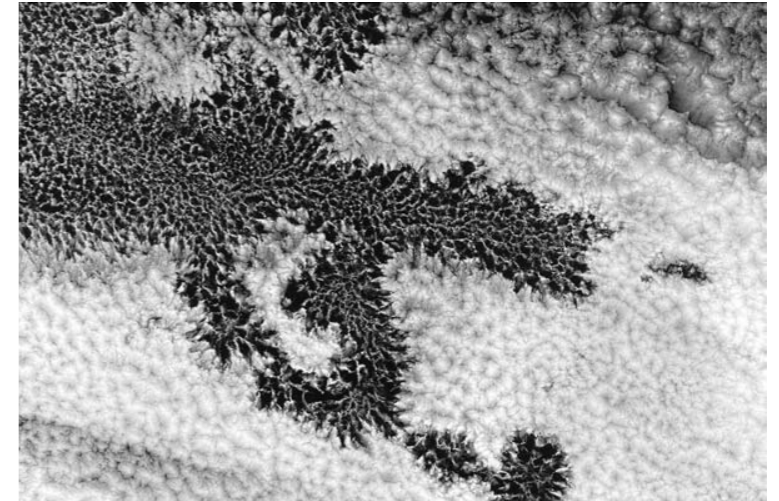
Deep Convection
(TRMM LBA)



Shallow Convection
(Bomex)



Stratocumulus
(DYCOMS RF01)



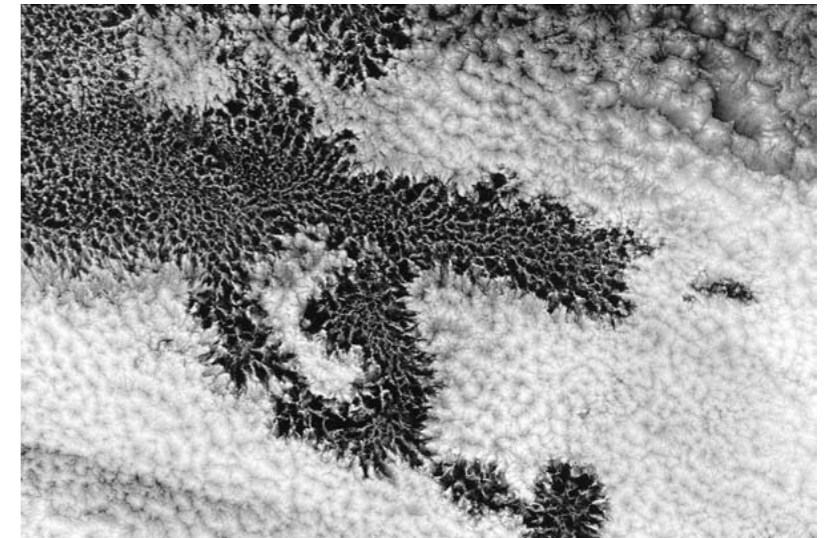
Deep Convection



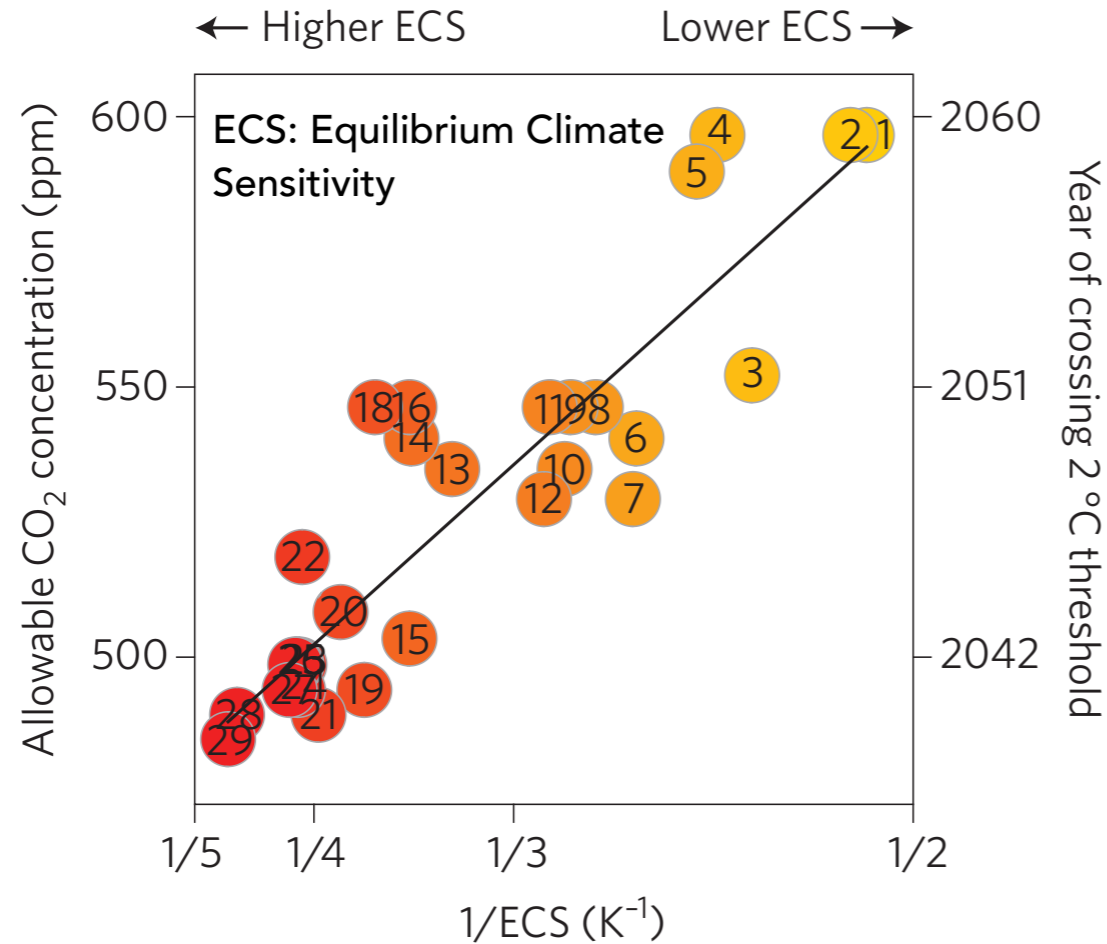
Shallow Convection



Stratocumulus



How much CO₂ can we emit to stay below the 2°C threshold?



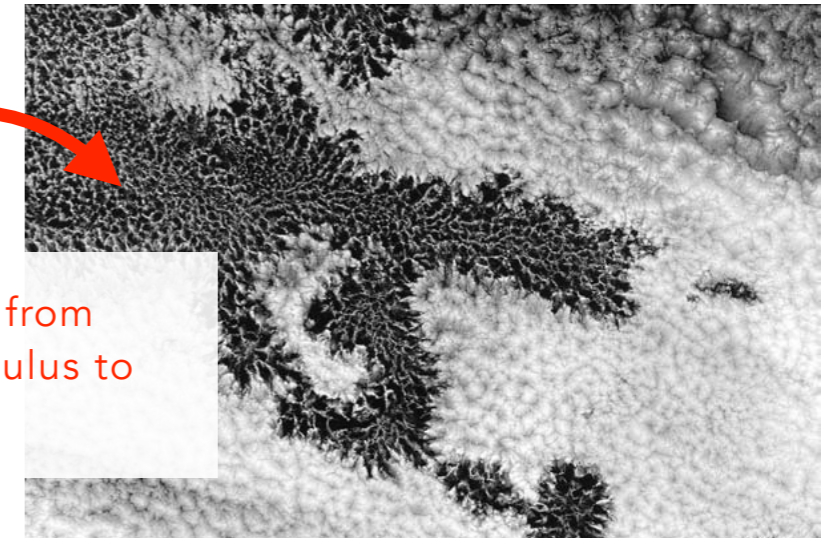
Deep Convection



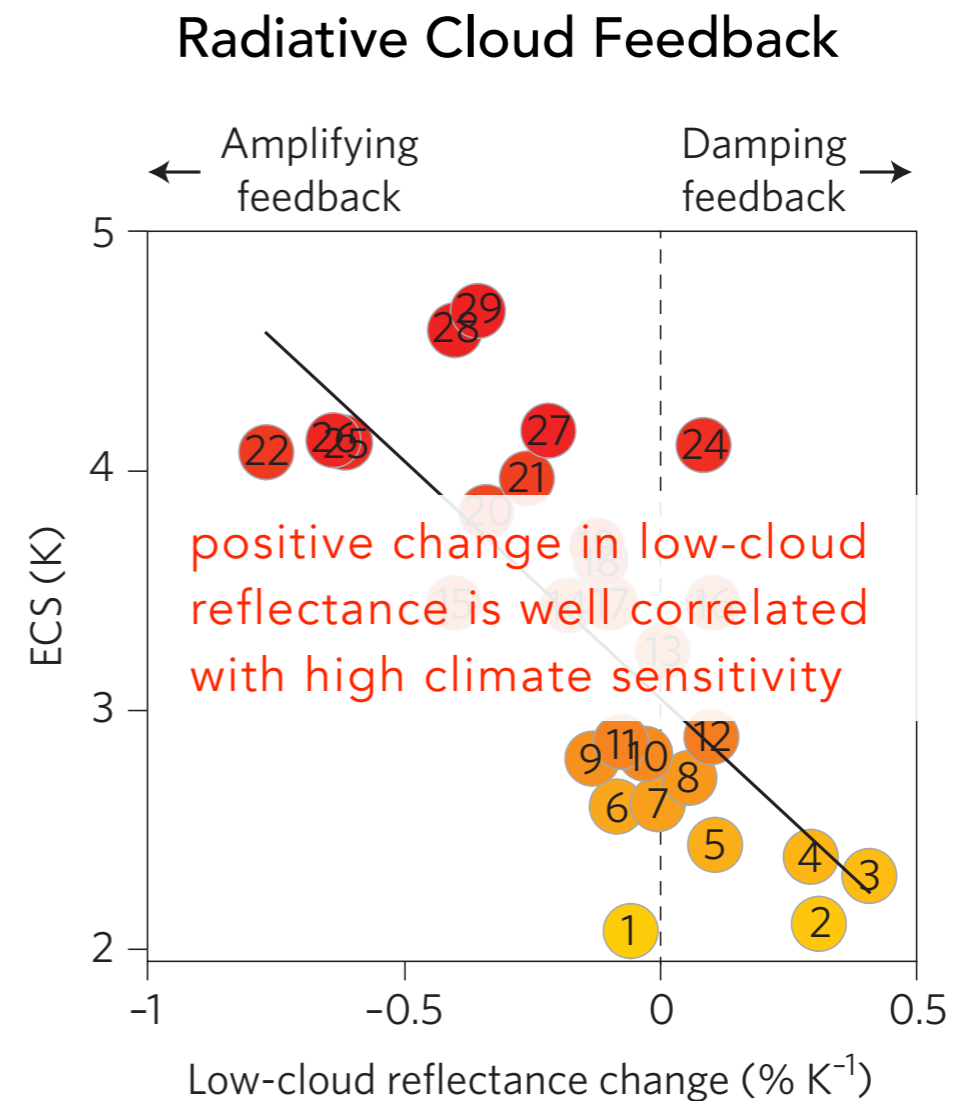
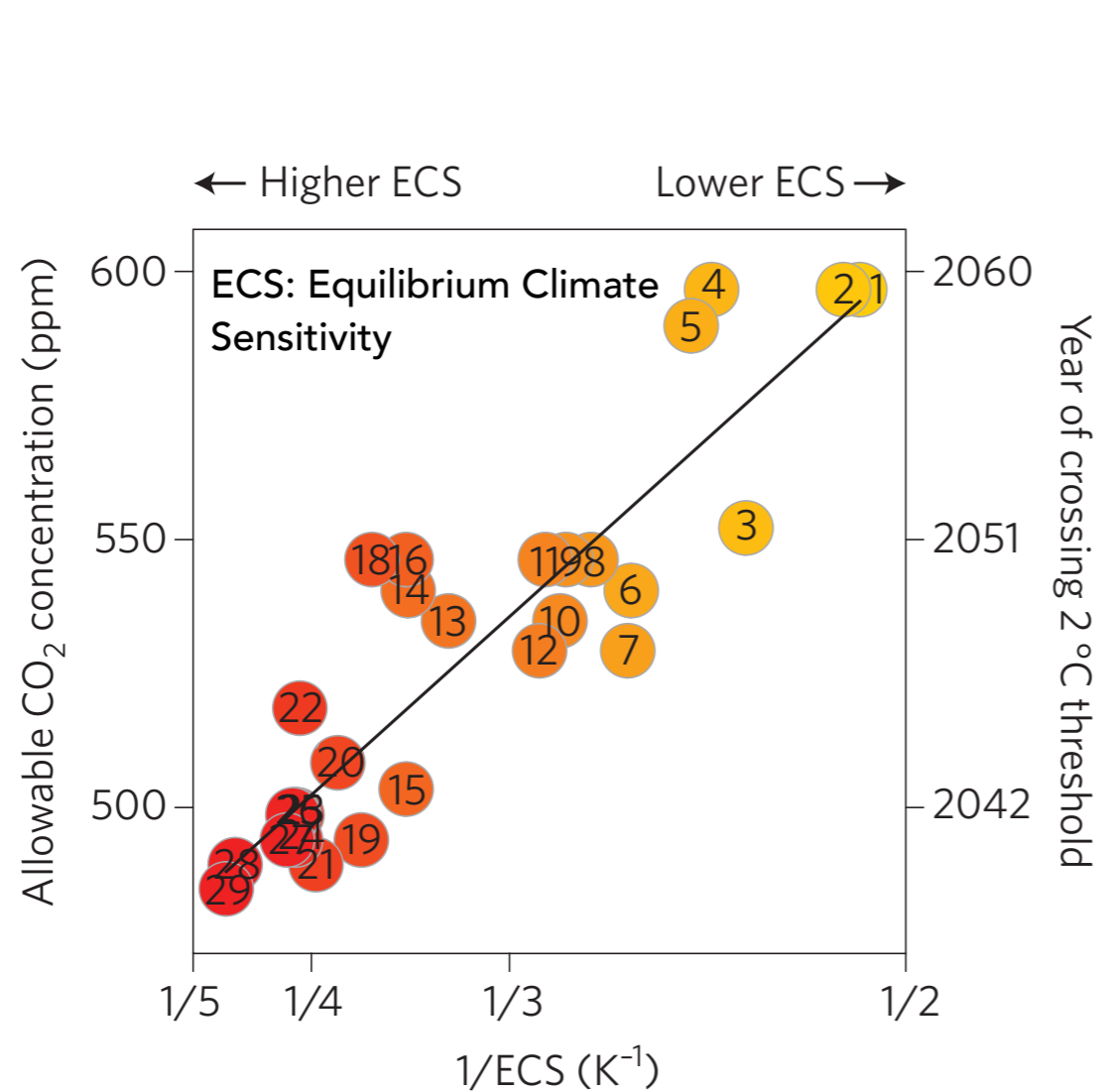
Shallow Convection



Stratocumulus



transition from stratocumulus to cumulus



2. BACKGROUND & CLIMATE MODELS

Equations of Motion (Navier-Stokes Equations)

Mass Continuity Equation

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0.$$

\mathbf{v} : velocity vector
 ρ : density

If density is constant this reduces to $\nabla \cdot \mathbf{v} = 0$.

Momentum Equation

$$\frac{D\mathbf{v}}{Dt} = -\frac{\nabla p}{\rho} + \nu \nabla^2 \mathbf{v} + \mathbf{F},$$

p : pressure, density
 \mathbf{F} : body forces (e.g., gravity)
 ν : viscosity

If density is constant, or pressure is given as a function of density alone (e.g., $p = C\rho^\gamma$), then (EOM.1) and (EOM.2) form a complete system.

Irreversible sink / source terms

Thermodynamic Equation

$$\frac{DI}{Dt} + \frac{p}{\rho} \nabla \cdot \mathbf{v} = \dot{Q}, \quad \text{or} \quad \frac{D\theta}{Dt} = \frac{1}{c_p} \left(\frac{\theta}{T} \right) \dot{Q},$$

I : internal energy
 θ : potential temperature
 \dot{Q} : diabatic sources (heating, diffusion)
 p, ρ : pressure, density

condensational heating: $Q_{cond} = -L_c \frac{Dw_s}{Dt},$

w_s : liquid water content, snow, ice (condensed phases)

radiation: $Q_{rad} = Q^{LW} + Q^{SW}$

$Q_{rad} = f(\rho(z))$, where ρ strongly depends on atmospheric composition and aerosols

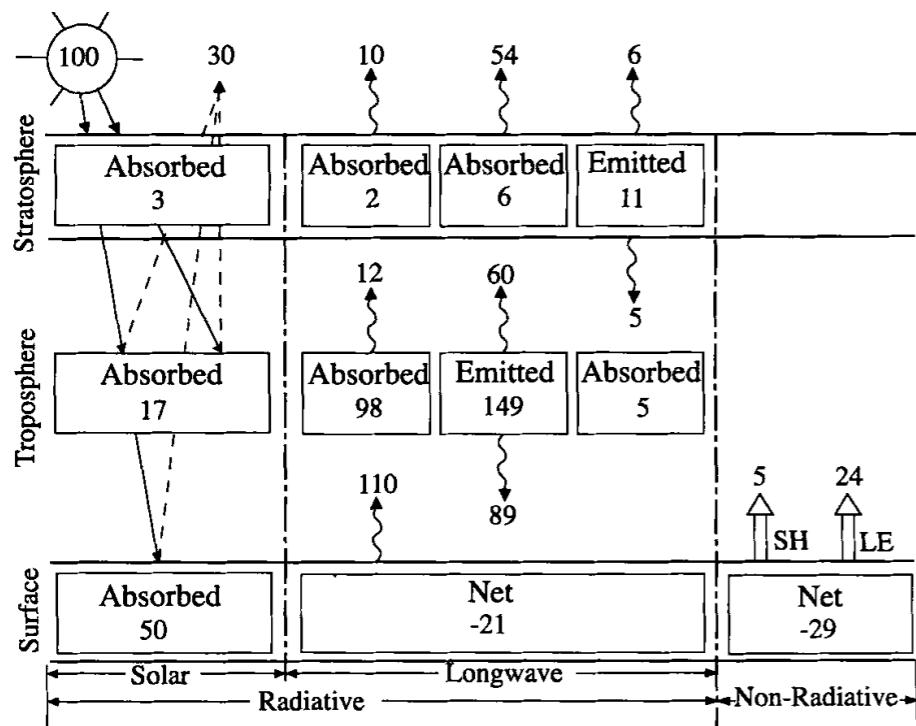
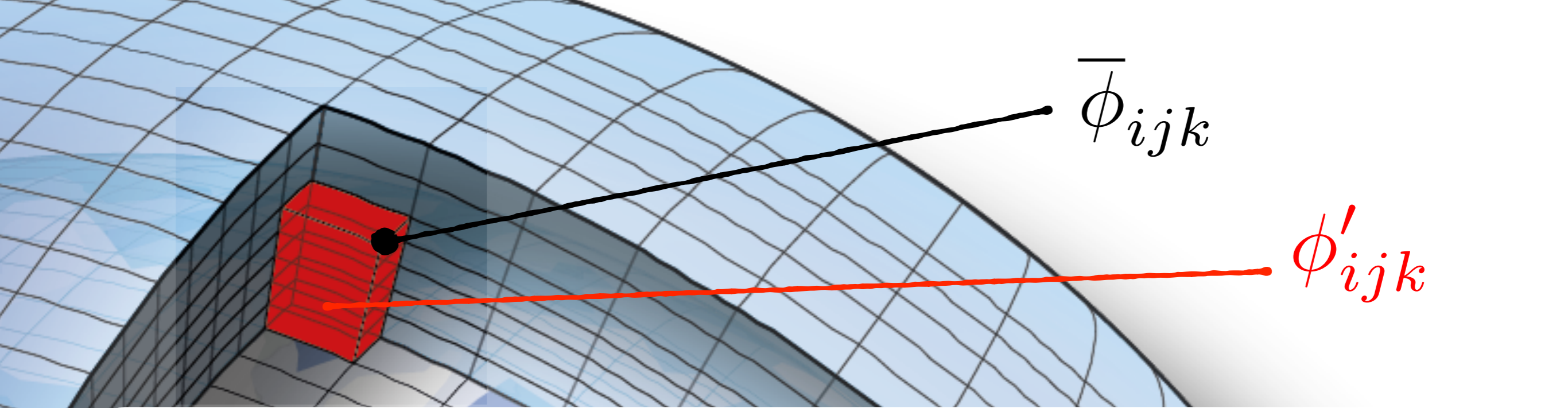


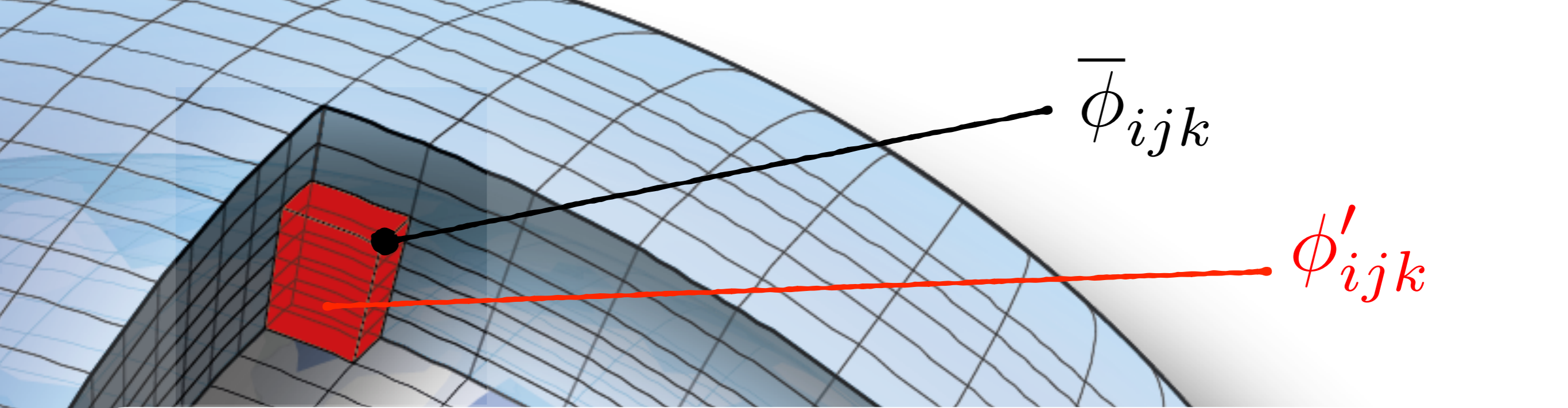
Fig. 2.4 Radiative and nonradiative energy flow diagram for Earth and its atmosphere. Units are percentages of the global-mean insolation (100 units = 342 W m⁻²).



$$\phi = \bar{\phi} + \phi', \quad \phi \in \{u, v, w, \theta, q_t\}$$

$$\bar{(\cdot)} := \int_{x_0}^{x_0+\Delta x} \int_{y_0}^{y_0+\Delta y} dx dy (\cdot).$$

total field: $\partial_t \phi = -(\vec{v} \cdot \nabla) \phi + F_\phi$

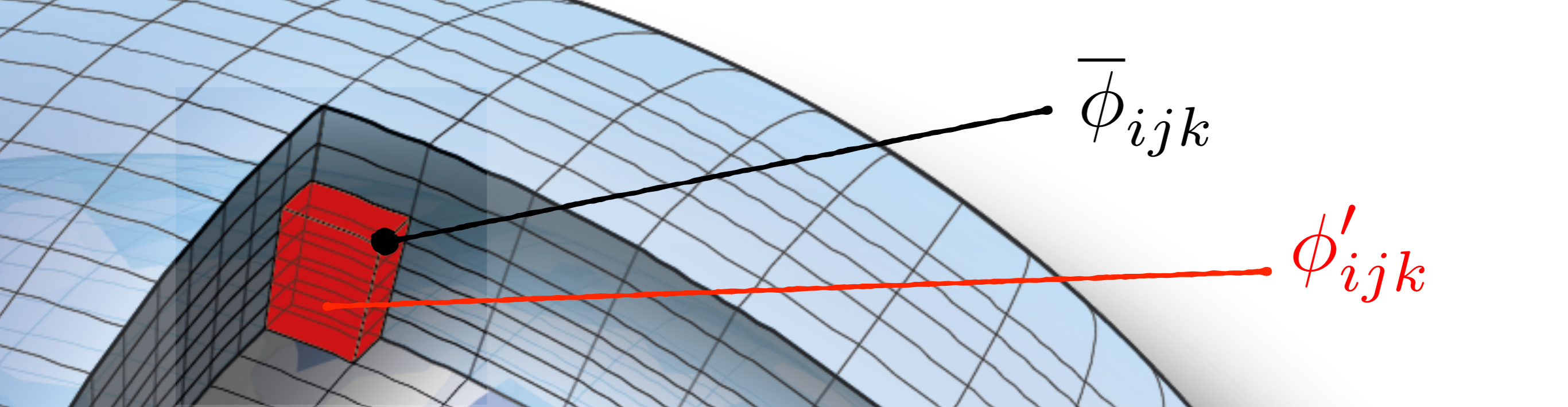


$$\phi = \bar{\phi} + \phi', \quad \phi \in \{u, v, w, \theta, q_t\}$$

$$\bar{(\cdot)} := \int_{x_0}^{x_0+\Delta x} \int_{y_0}^{y_0+\Delta y} dx dy (\cdot).$$

total field: $\partial_t \phi = -(\vec{v} \cdot \nabla) \phi + F_\phi$

$$= - [(\bar{\vec{v}} \cdot \nabla) \bar{\phi} + (\bar{\vec{v}} \cdot \nabla) \phi' + (\vec{v}' \cdot \nabla) \bar{\phi} + (\vec{v}' \cdot \nabla) \phi'] + F_\phi$$

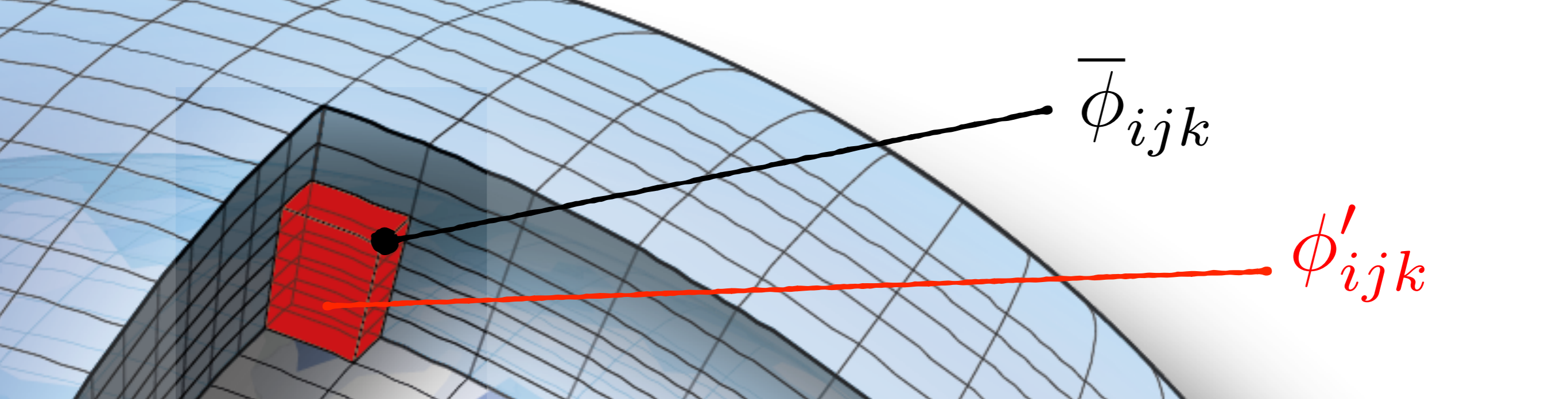


$$\phi = \bar{\phi} + \phi', \quad \phi \in \{u, v, w, \theta, q_t\}$$

$$\bar{(\cdot)} := \int_{x_0}^{x_0+\Delta x} \int_{y_0}^{y_0+\Delta y} dx dy (\cdot).$$

total field: $\partial_t \phi = -(\vec{v} \cdot \nabla) \phi + F_\phi$
 $= - [(\bar{\vec{v}} \cdot \nabla) \bar{\phi} + (\bar{\vec{v}} \cdot \nabla) \phi' + (\vec{v}' \cdot \nabla) \bar{\phi} + (\vec{v}' \cdot \nabla) \phi'] + F_\phi$

resolved field: $\partial_t \bar{\phi} = -(\bar{\vec{v}} \cdot \nabla) \bar{\phi} - \overline{(\vec{v}' \cdot \nabla) \phi'} + \bar{F}_\phi$



$$\phi = \bar{\phi} + \phi', \quad \phi \in \{u, v, w, \theta, q_t\}$$

$$\bar{(\cdot)} := \int_{x_0}^{x_0+\Delta x} \int_{y_0}^{y_0+\Delta y} dx dy (\cdot).$$

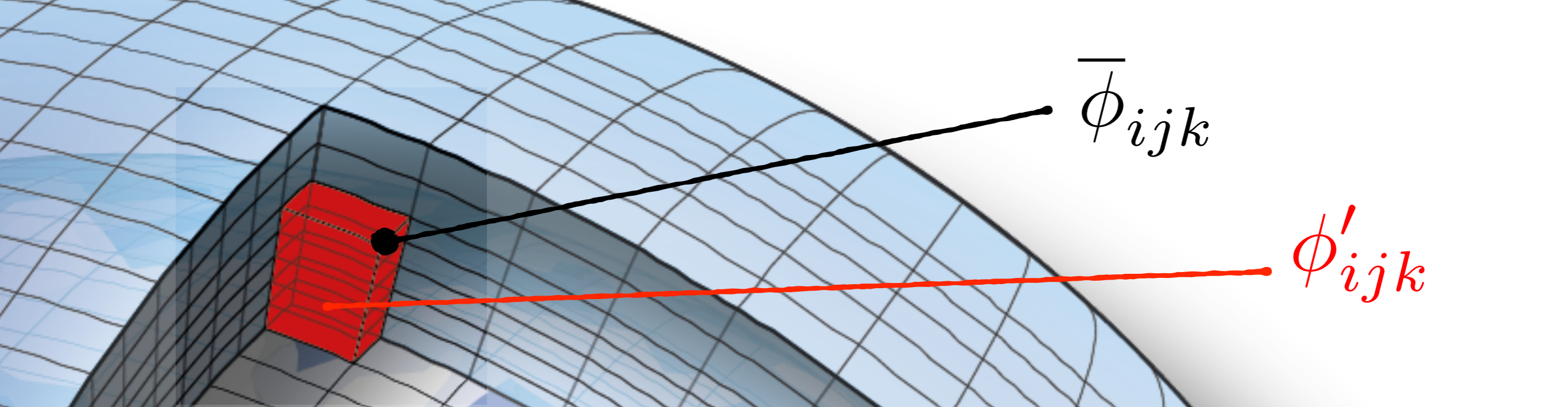
total field: $\partial_t \phi = -(\vec{v} \cdot \nabla) \phi + F_\phi$

$$= - [(\bar{\vec{v}} \cdot \nabla) \bar{\phi} + (\bar{\vec{v}} \cdot \nabla) \phi' + (\vec{v}' \cdot \nabla) \bar{\phi} + (\vec{v}' \cdot \nabla) \phi'] + F_\phi$$

resolved field: $\partial_t \bar{\phi} = -(\bar{\vec{v}} \cdot \nabla) \bar{\phi} - \overline{(\vec{v}' \cdot \nabla) \phi'} + \bar{F}_\phi$

Reynolds Stress

sub-grid scale field: $\partial_t \phi' + (\bar{\vec{v}} \cdot \nabla) \phi' + (\vec{v}' \cdot \nabla) \phi' + [(\vec{v}' \cdot \nabla) \phi' - \overline{(\vec{v}' \cdot \nabla) \phi'}] = F'_\phi$



$$\phi = \bar{\phi} + \phi', \quad \phi \in \{u, v, w, \theta, q_t\}$$

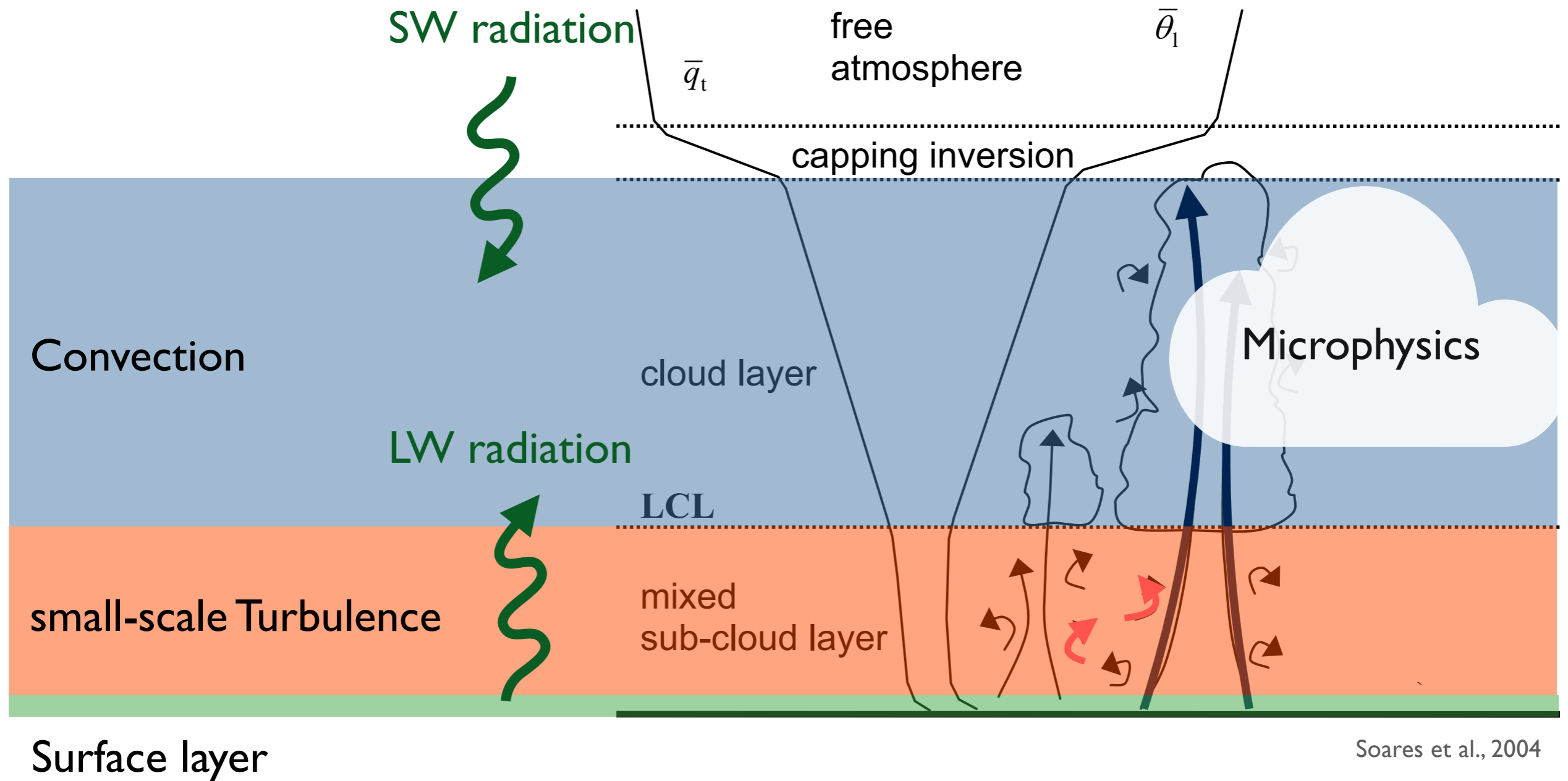
$$\bar{(\cdot)} := \int_{x_0}^{x_0+\Delta x} \int_{y_0}^{y_0+\Delta y} dx dy (\cdot).$$

total field: $\partial_t \phi = -(\vec{v} \cdot \nabla) \phi + F_\phi$
 $= - [(\bar{\vec{v}} \cdot \nabla) \bar{\phi} + (\bar{\vec{v}} \cdot \nabla) \phi' + (\vec{v}' \cdot \nabla) \bar{\phi} + (\vec{v}' \cdot \nabla) \phi'] + F_\phi$

resolved field: $\partial_t \bar{\phi} = -(\bar{\vec{v}} \cdot \nabla) \bar{\phi} - \overline{(\vec{v}' \cdot \nabla) \phi'} + \bar{F}_\phi$ **Reynolds Stress**

sub-grid scale field: $\partial_t \phi' + (\bar{\vec{v}} \cdot \nabla) \phi' + (\vec{v}' \cdot \nabla) \phi' + [(\vec{v}' \cdot \nabla) \phi' - \overline{(\vec{v}' \cdot \nabla) \phi'}] = F'_\phi$

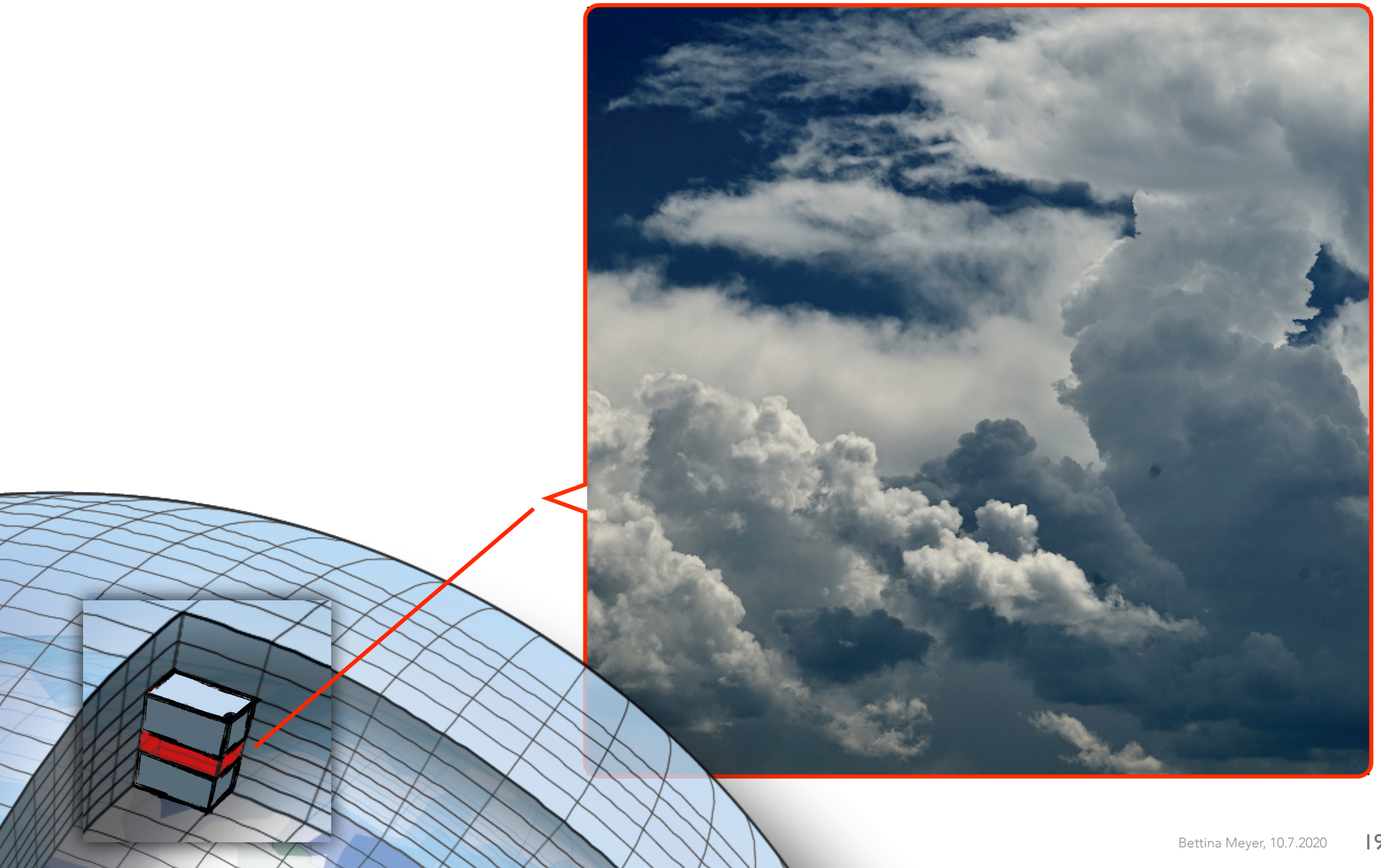
Sub-Grid Scale Parameterisations



Soares et al., 2004

3. CLOUD MICROPHYSICS

Cloud Schemes



Irreversible sink / source terms

Thermodynamic Equation

$$\frac{DI}{Dt} + \frac{p}{\rho} \nabla \cdot \mathbf{v} = \dot{Q}, \quad \text{or} \quad \frac{D\theta}{Dt} = \frac{1}{c_p} \left(\frac{\theta}{T} \right) \dot{Q},$$

I : internal energy

θ : potential temperature

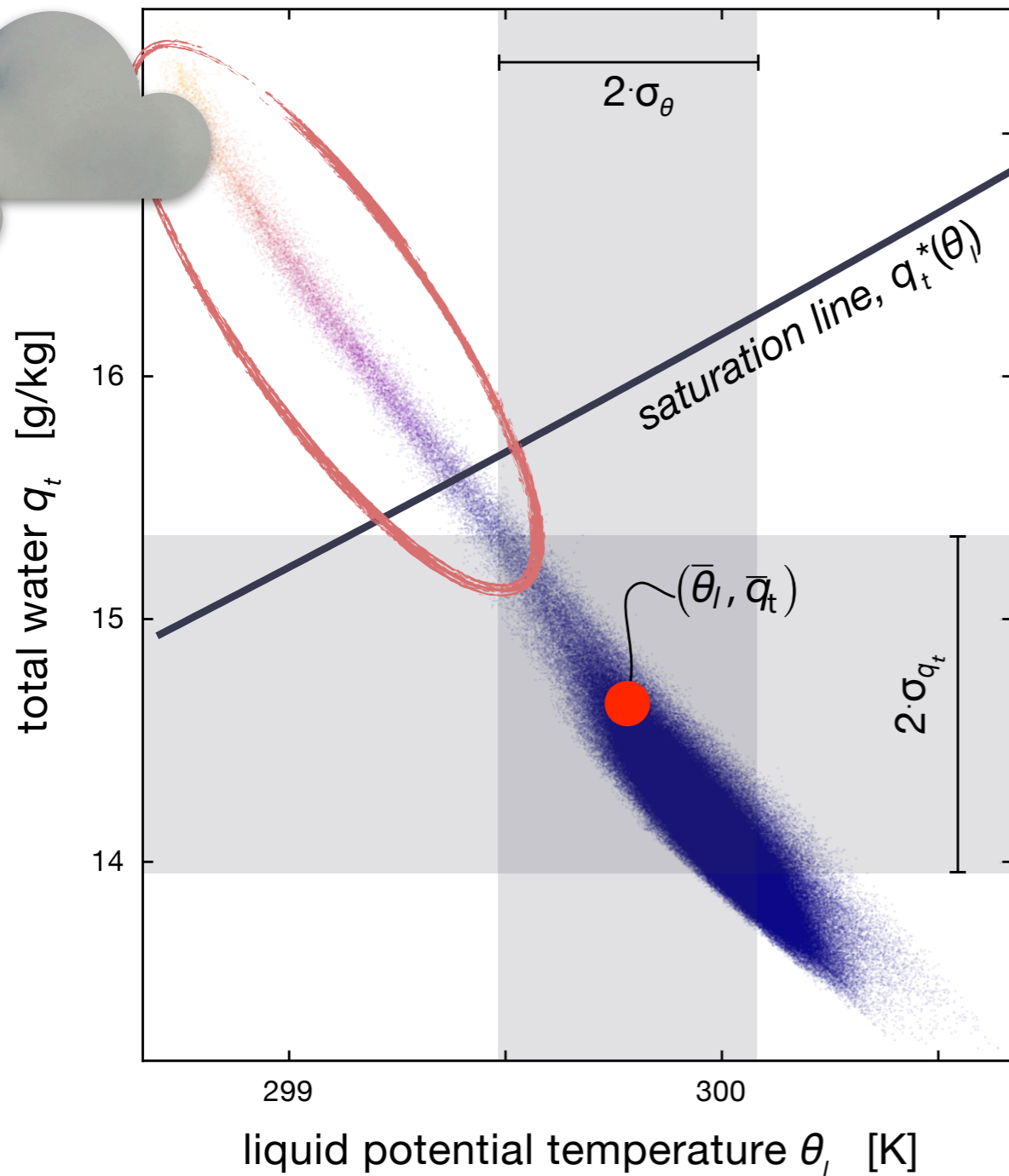
\dot{Q} : diabatic sources (heating, diffusion)

p, ρ : pressure, density

condensational heating: $Q_{cond} = -L_c \frac{Dw_s}{Dt},$

w_s : liquid water, snow and ice content
(condensed phases)

Cloud Schemes



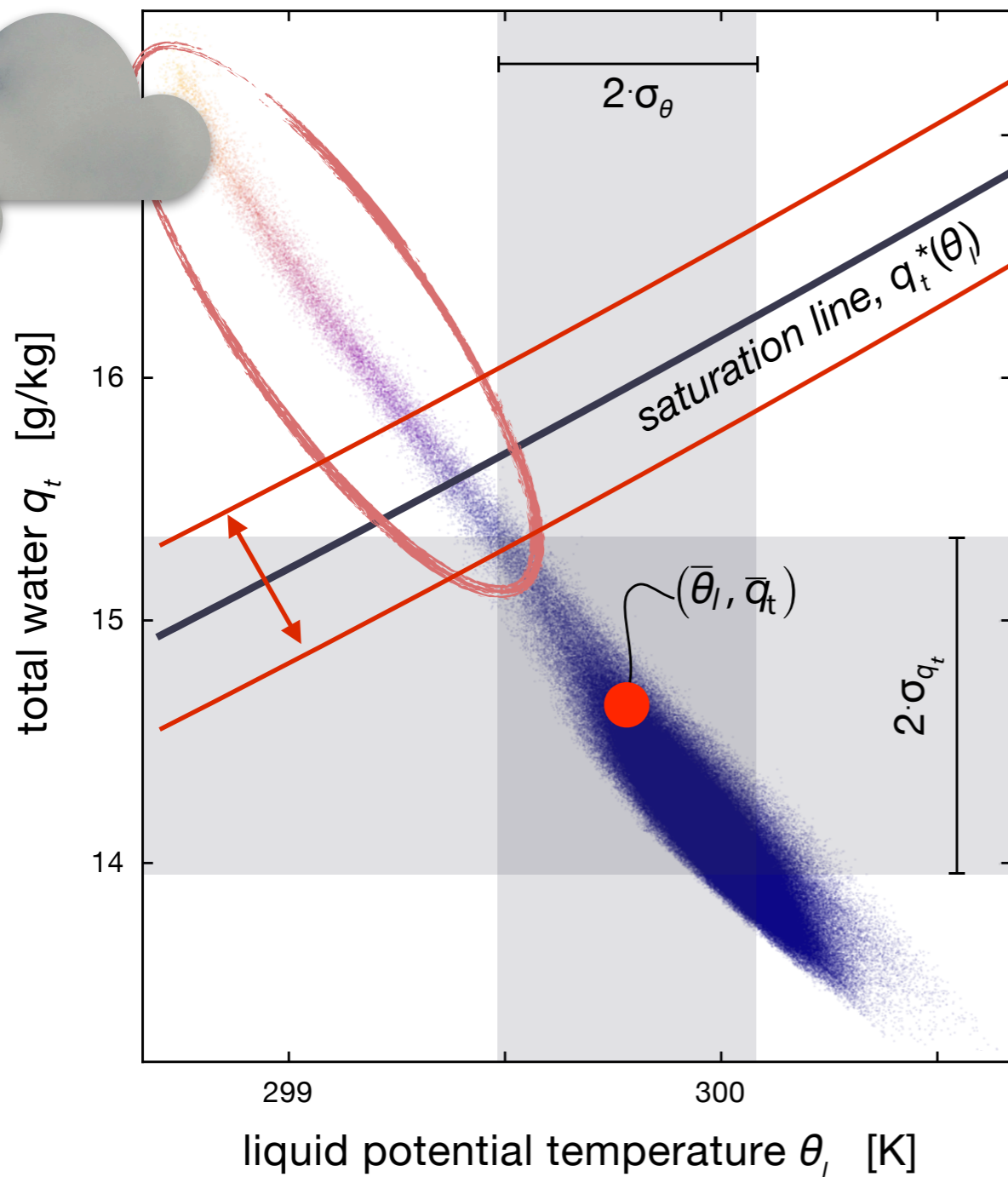
Data, sampled from a large-eddy simulation of a shallow convection (BOMEX) cloud layer ($z = 800\text{m}$), accumulated over one hour.

The colouring indicates the liquid water content.

liquid potential temperature:

$$\bar{\theta}_l \approx \theta \left(1 - \frac{r_l}{\epsilon + r_t} \right)$$

Cloud Schemes

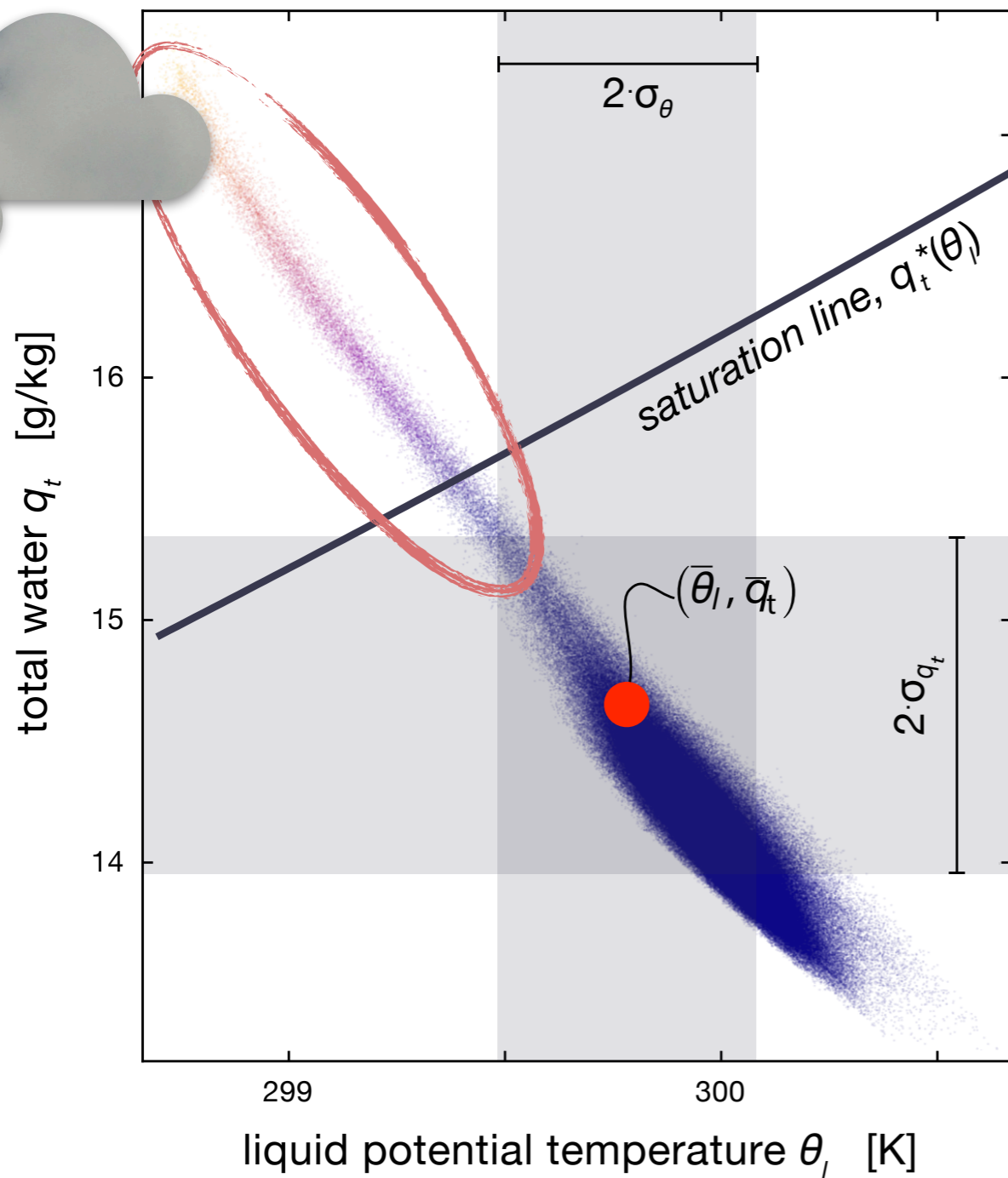


shallow convection (BOMEX) cloud layer ($z = 800\text{m}$);
colouring indicates liquid water content.

Saturation Line:

- equilibrium vs. non-equilibrium phase partitioning
 - equilibrium: either sub-saturated or at saturation
 - non-equilibrium: supersaturation, supercooled liquid
- nucleation: *homogeneous nucleation* (formation of a drop of pure water from vapour) vs. *heterogeneous nucleation* (collection of molecules onto a foreign substance).
>> aerosols (condensation nucleation)

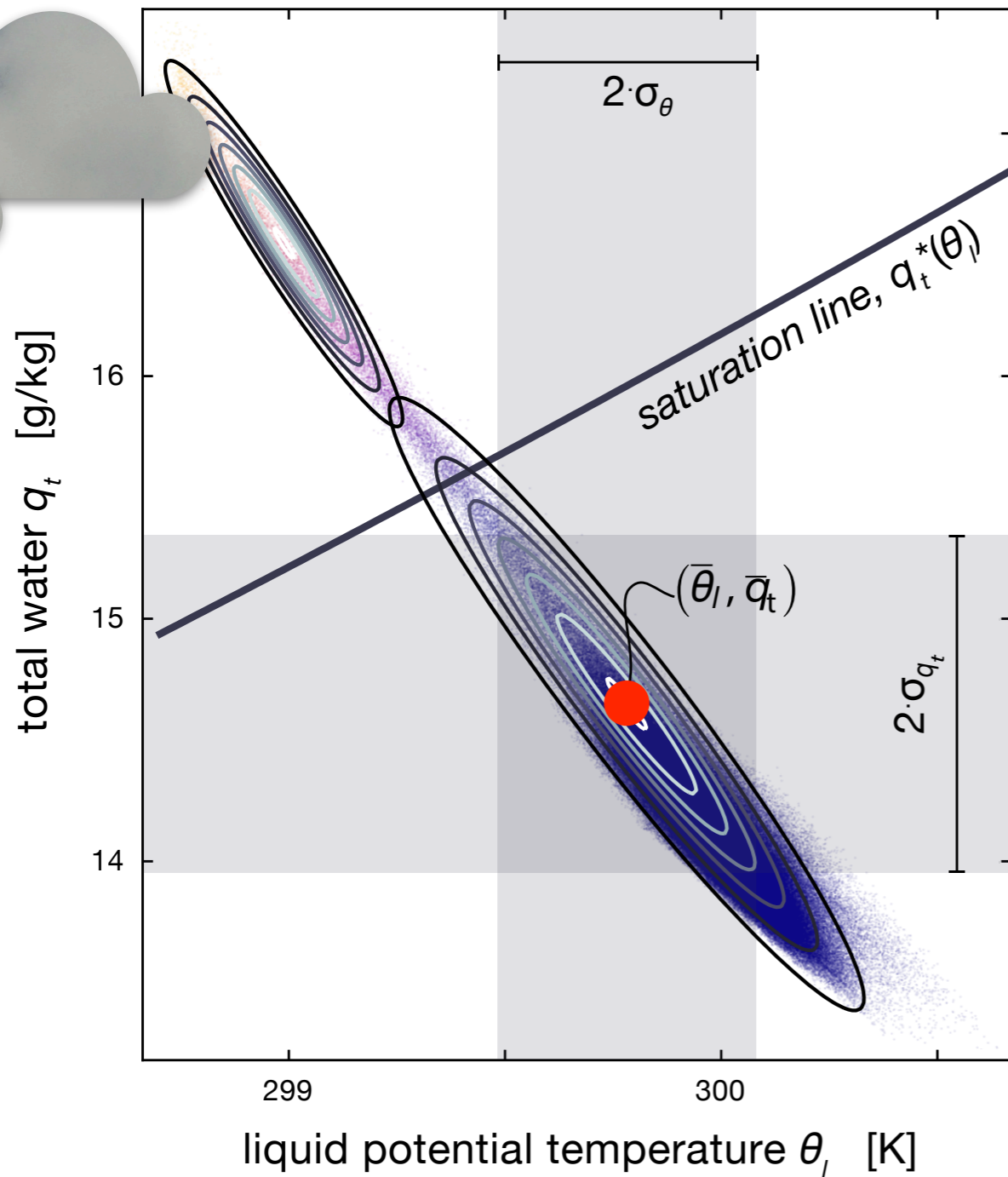
Cloud Schemes



- warm clouds: only liquid phase
- mixed phase cloud: liquid and ice phase (snow, graupel, ice)

shallow convection (BOMEX) cloud layer ($z = 800\text{m}$);
colouring indicates liquid water content.

Cloud Schemes



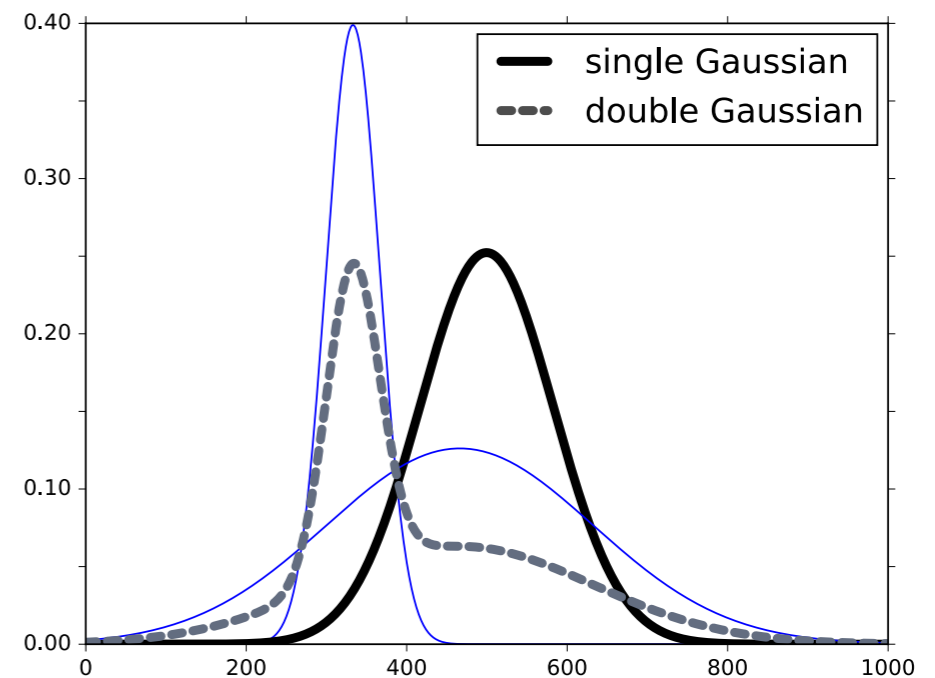
shallow convection (BOMEX) cloud layer ($z = 800\text{m}$); colouring indicates liquid water content.

Cloud Fraction:

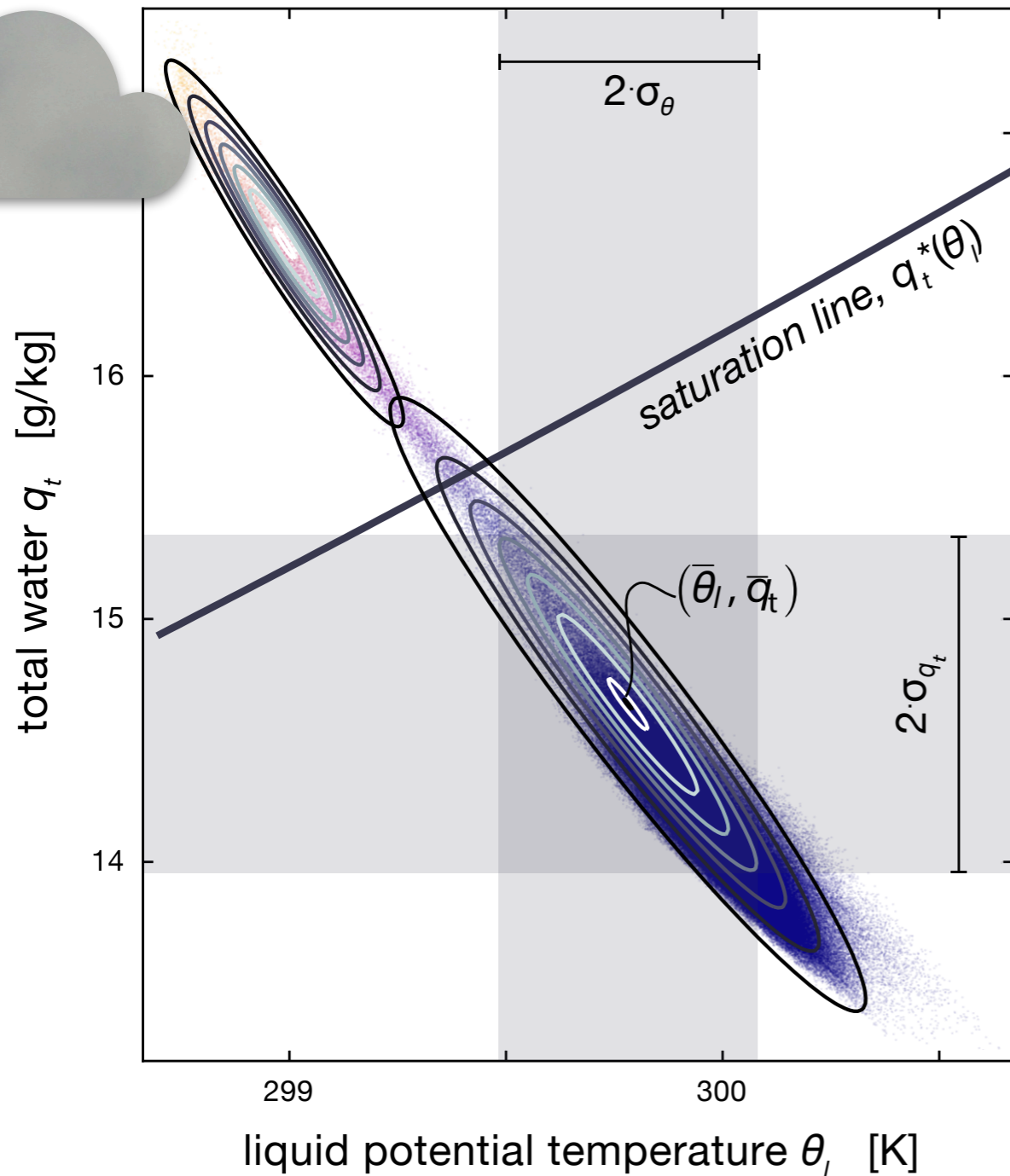
$$CF = \int_{-\infty}^{\infty} \int_{q_{l,s}}^{\infty} G(\theta_l, q_t) dq_t d\theta_l$$

Mean Liquid Water:

$$\bar{q}_l = \int_{-\infty}^{\infty} \int_{q_t^*}^{\infty} G(\theta_l, q_t) q_l(\theta_l, q_t) dq_t d\theta_l$$



Cloud Schemes

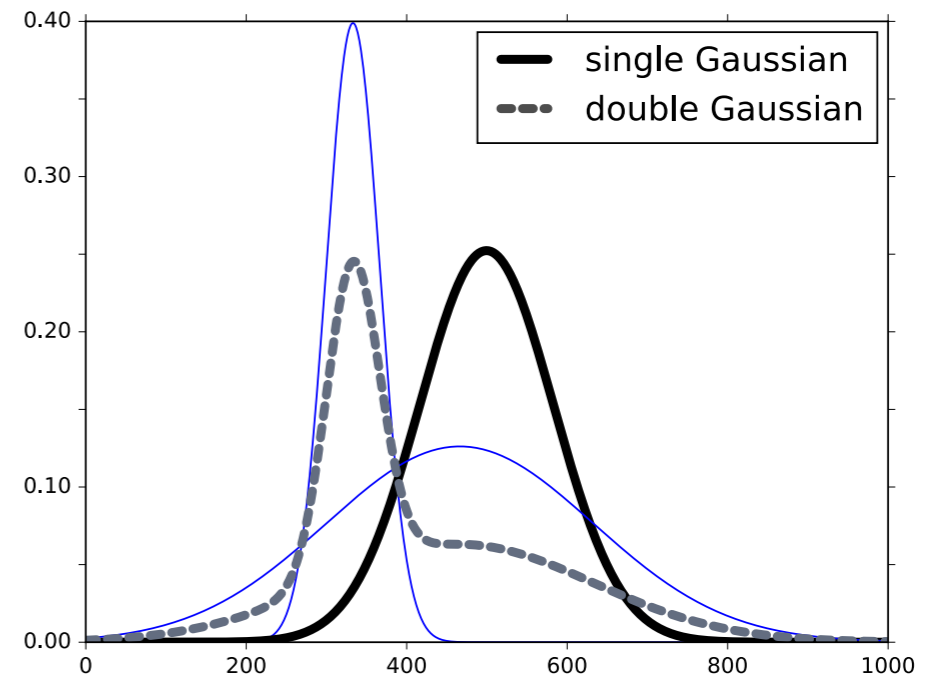


Cloud Fraction:

$$CF = \int_{-\infty}^{\infty} \int_{q_{l,s}}^{\infty} G(\theta_l, q_t) dq_t d\theta_l$$

Mean Liquid Water:

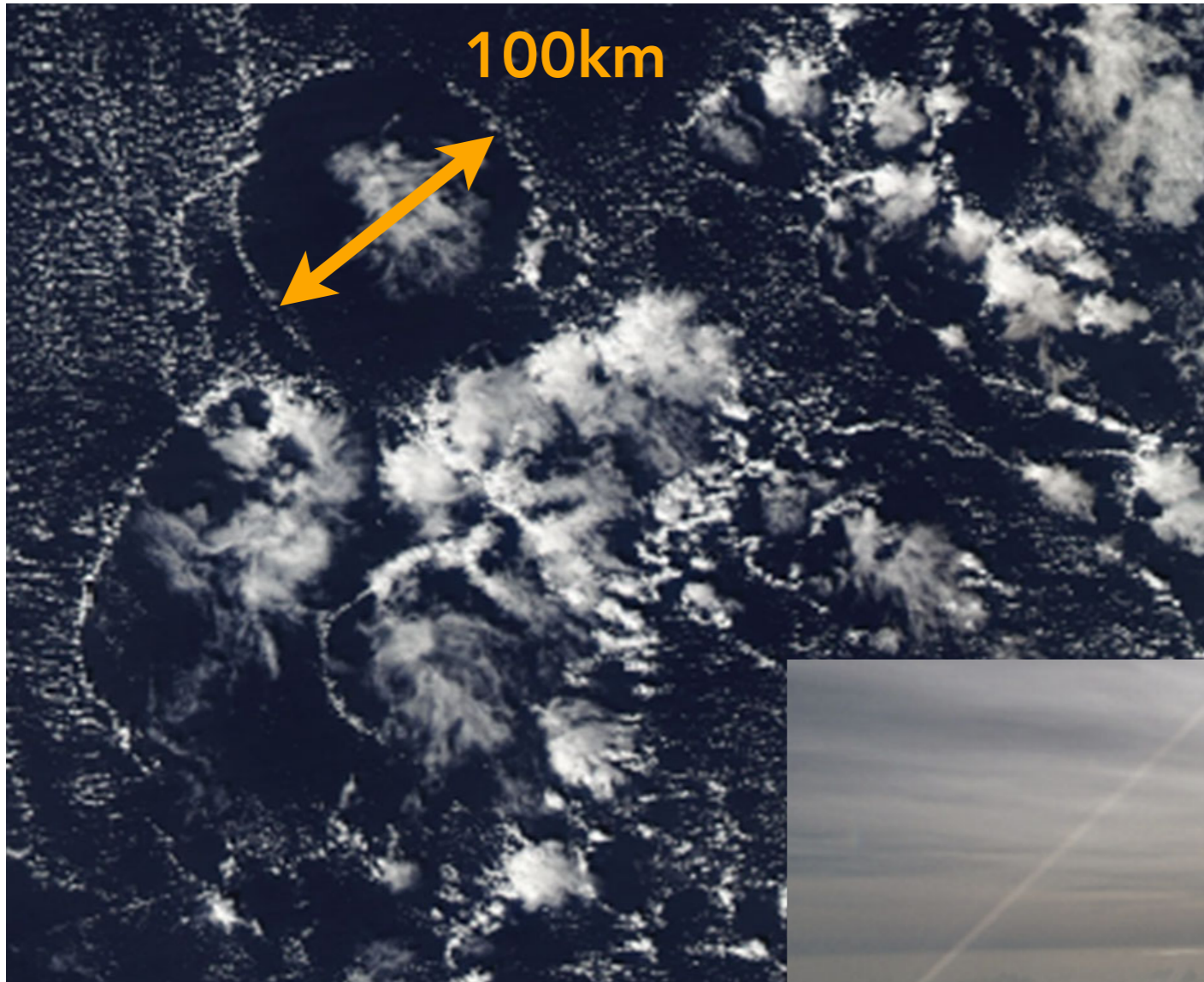
$$\bar{q}_l = \int_{-\infty}^{\infty} \int_{q_t^*}^{\infty} G(\theta_l, q_t) q_l(\theta_l, q_t) dq_t d\theta_l$$



Data, sampled from a shallow convection (BOMEX) cloud layer ($z = 800\text{m}$) and the coloring indicates the liquid water content.

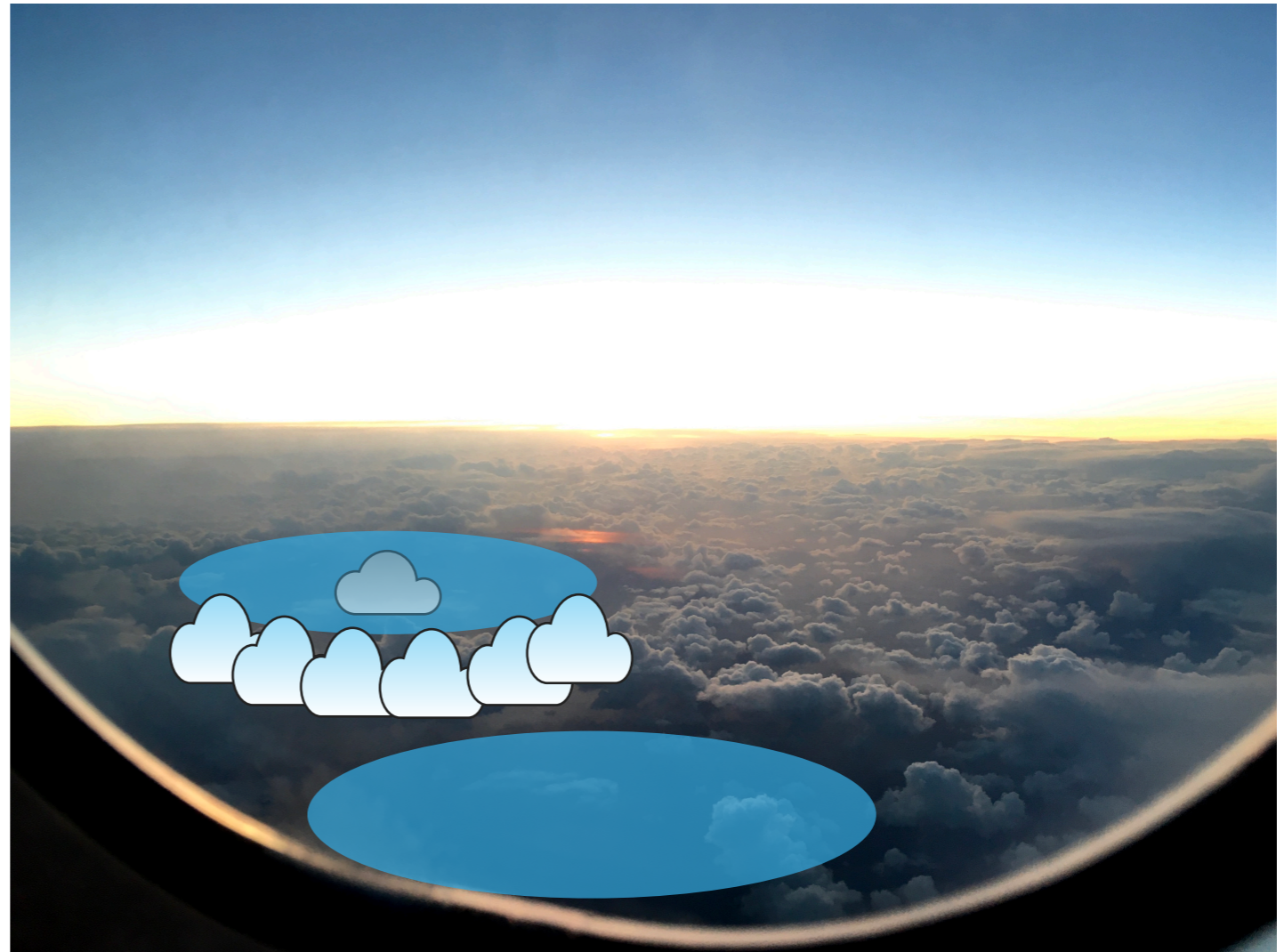
4. COLD POOLS

Cold Pools



Figures:
Zuidema et al., Surv Geophys (2017)
NASA / JPL-Caltech, S. Böing (2016)

Cold Pools



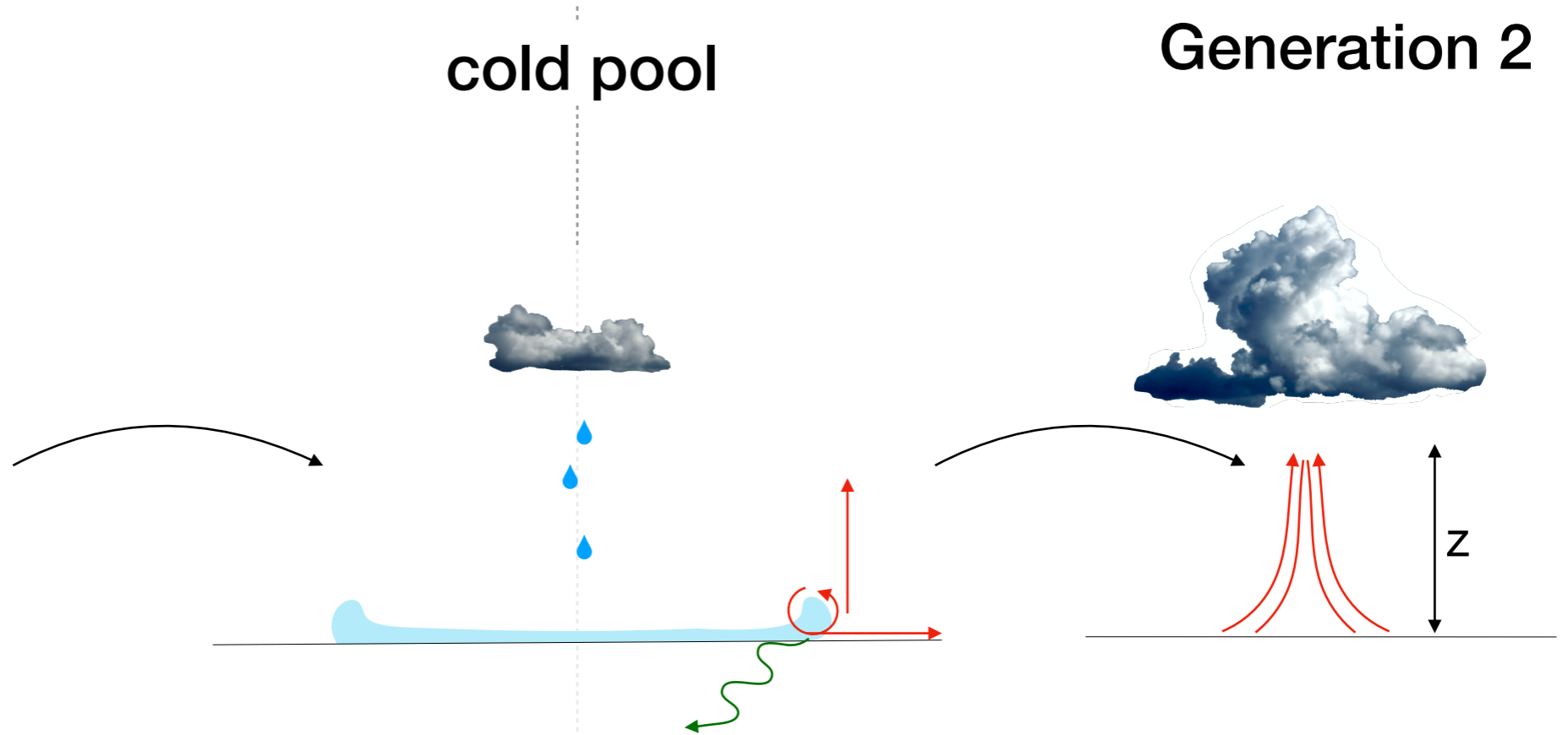
Cold Pools - Linking Clouds over Time and Space

Generation 1



Potential Energy
from evaporative
cooling

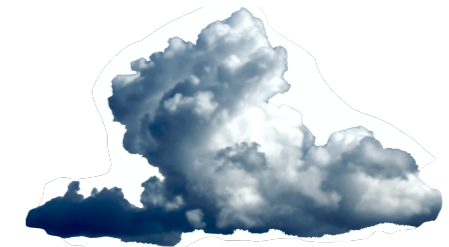
cold pool



Kinetic Energy:
CP rotation and
spreading,
ambient motion

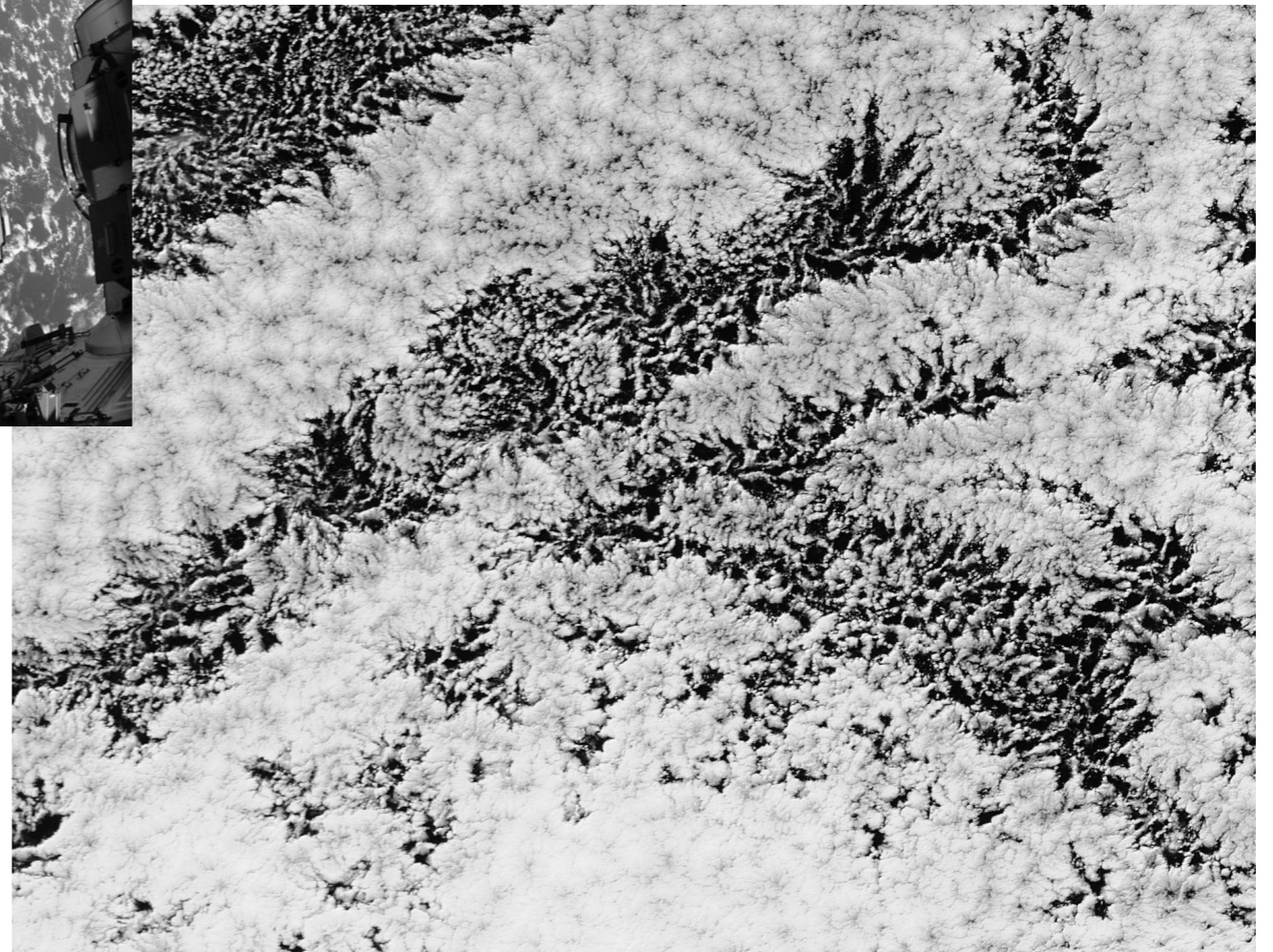
Energy Dissipation:
Friction, surface fluxes,
mixing

Generation 2



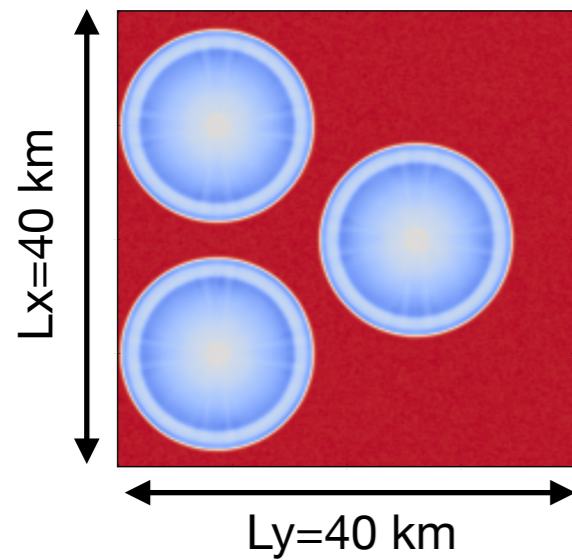
Potential Energy
to overcome CAPE,
transport of sensible
and latent heat

Cold Pools - Organisation of the Cloud Field

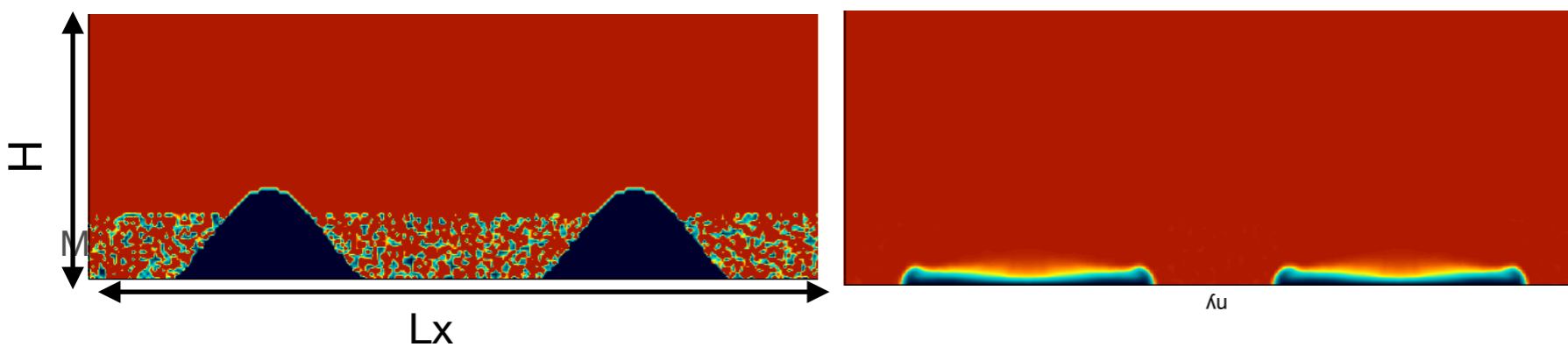
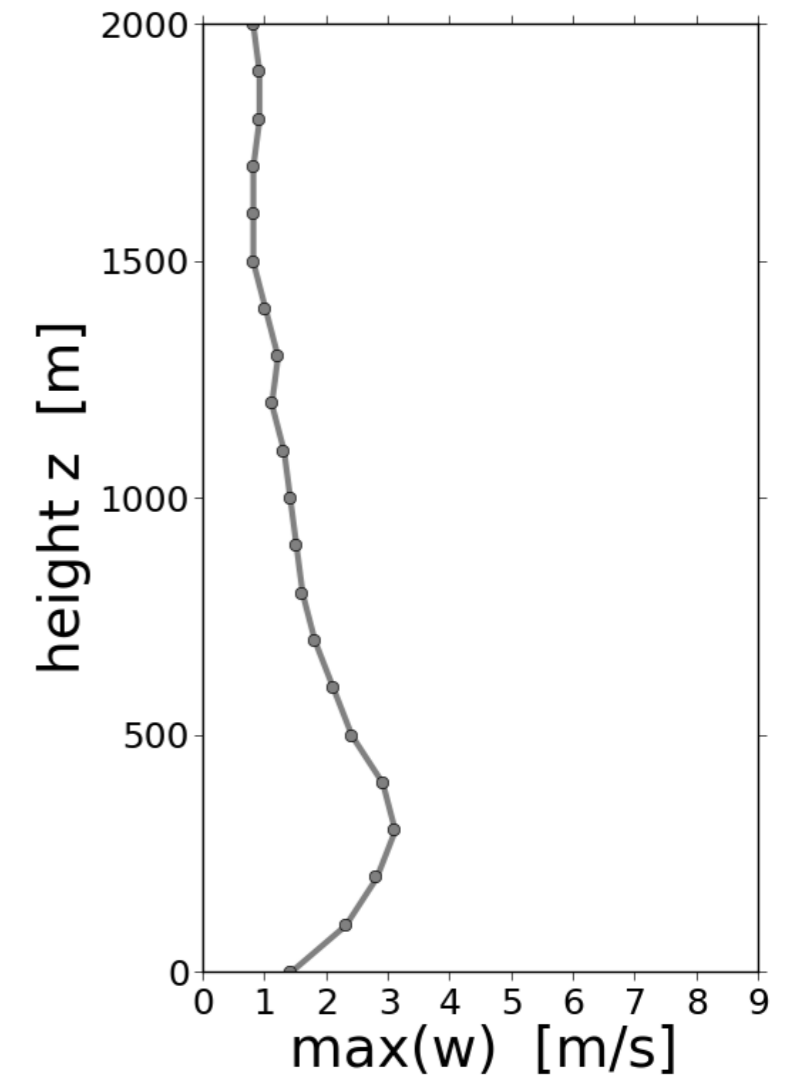


Figures:
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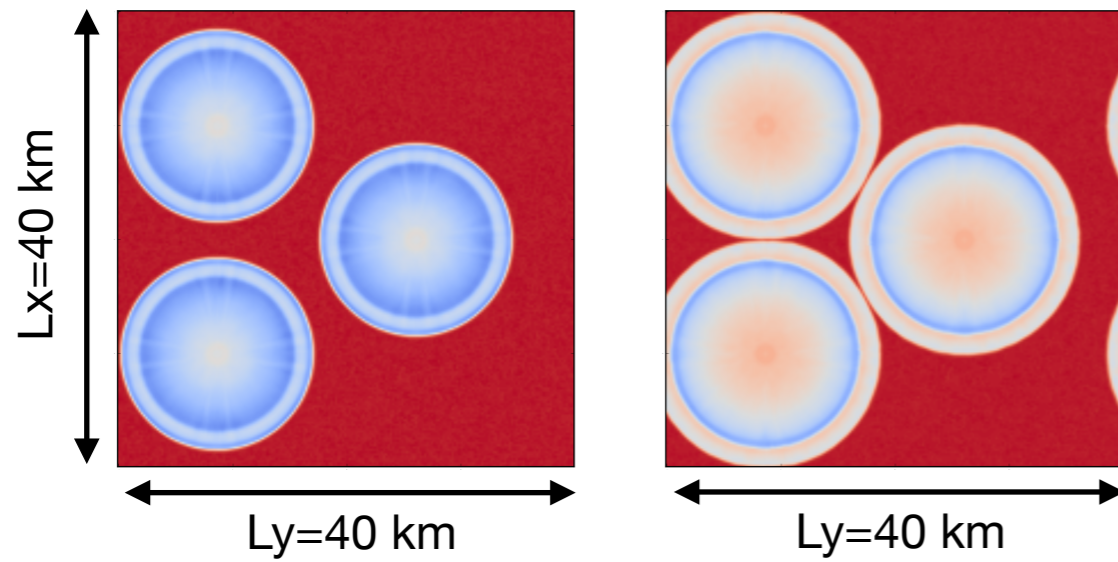
Vertical velocity - triple collision



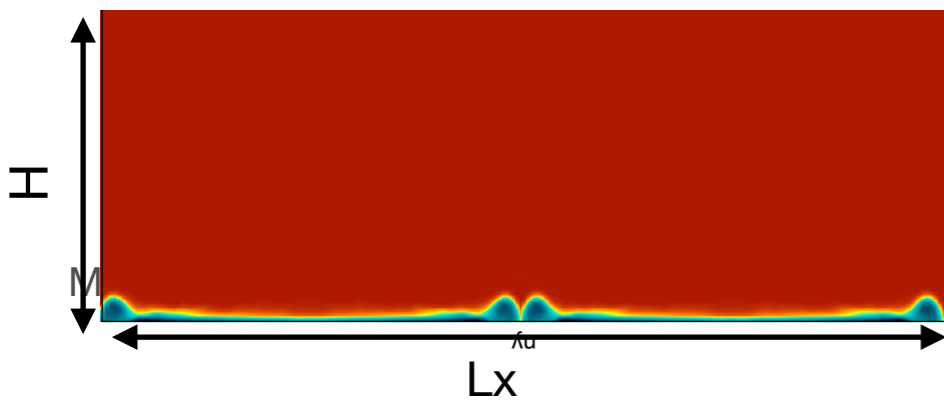
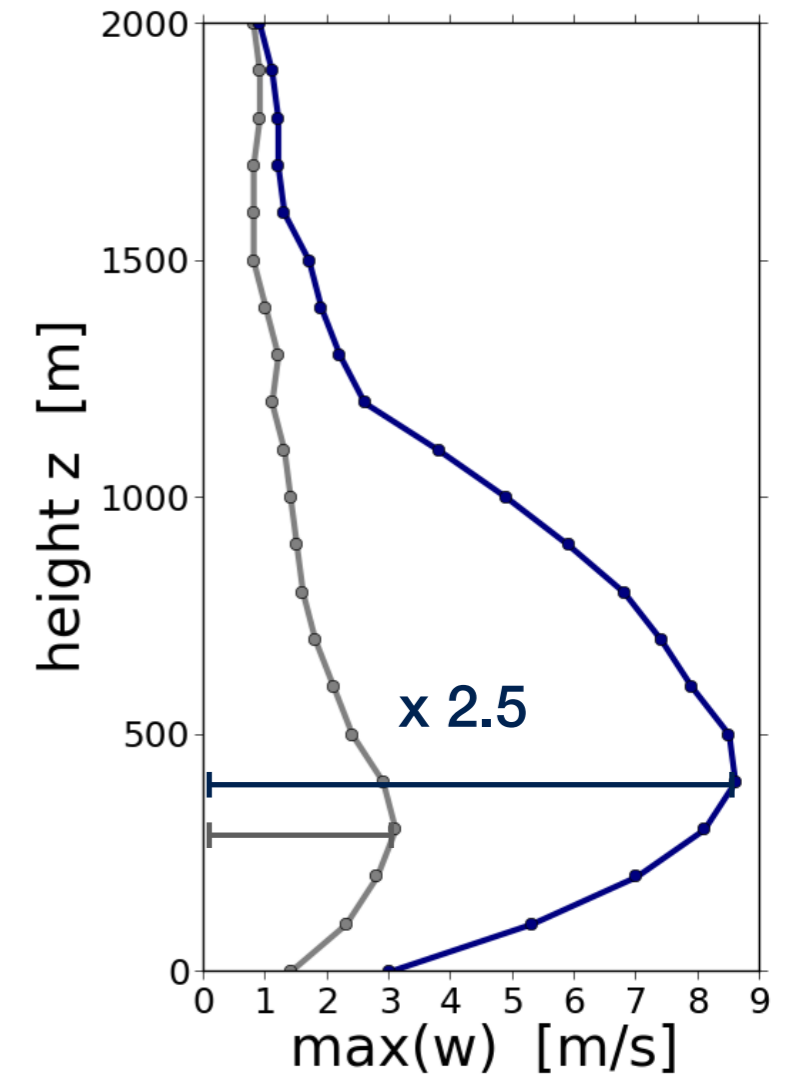
— single CP (undisturbed front)



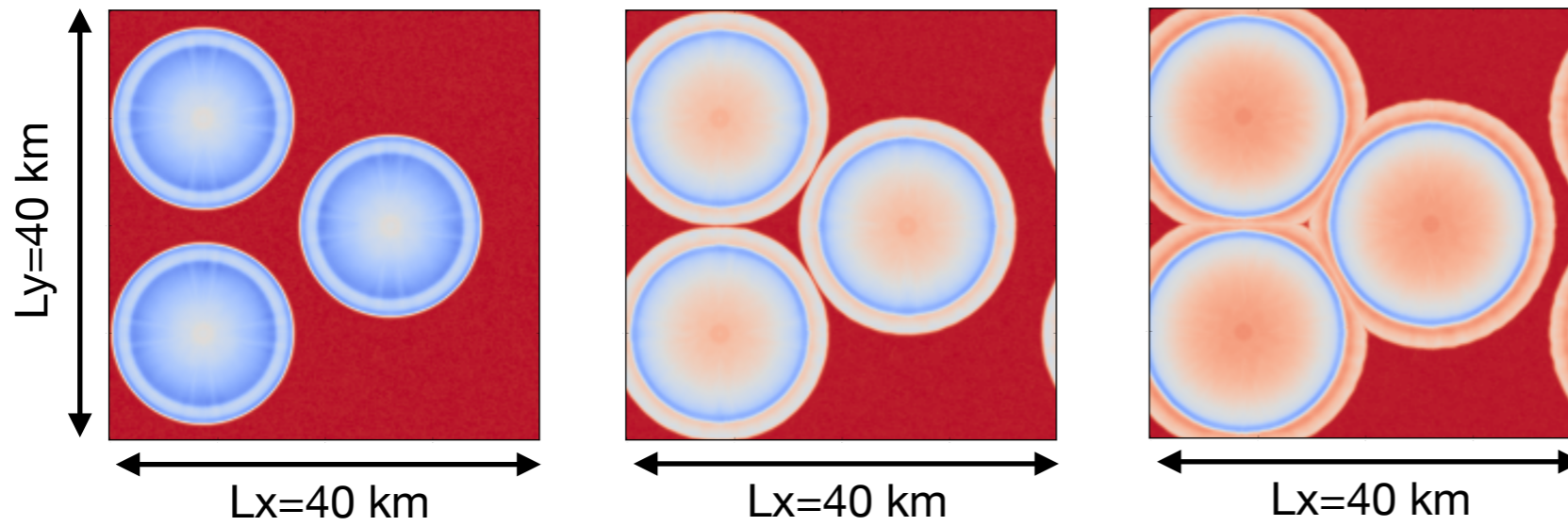
Vertical velocity - triple collision



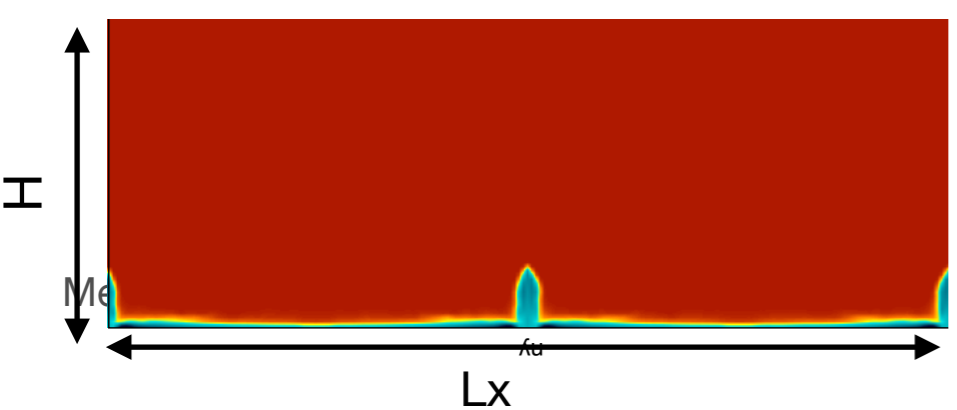
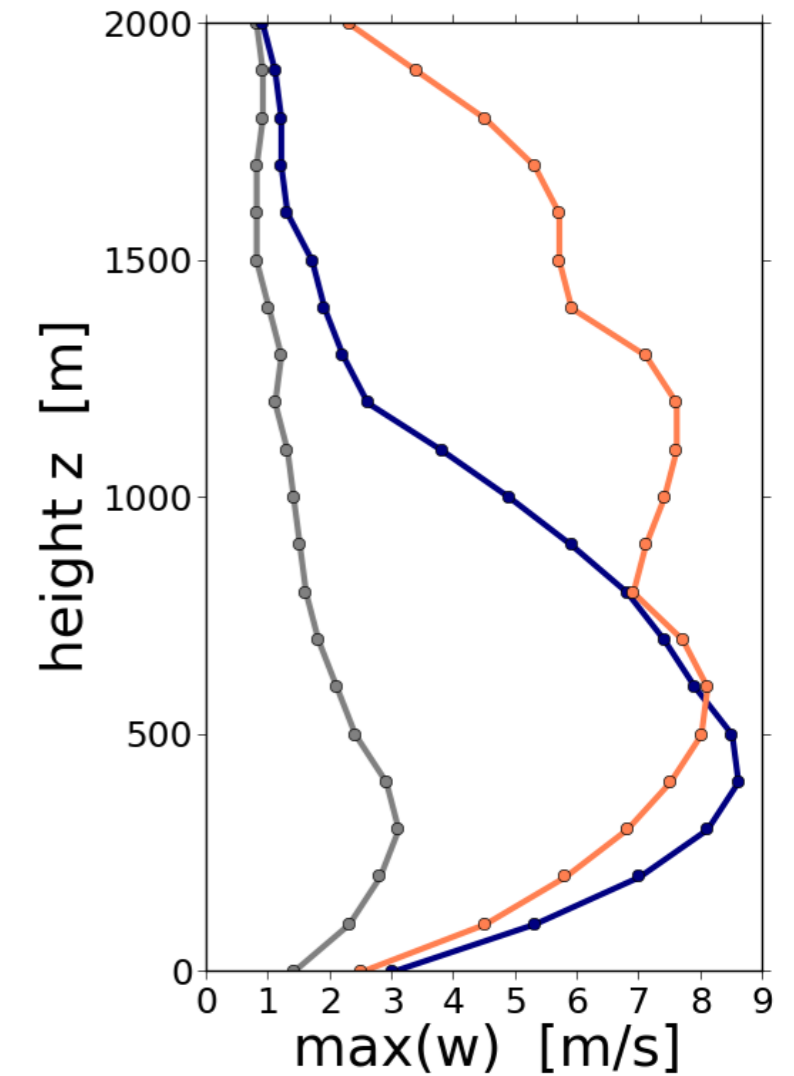
- single CP (undisturbed front)
- 2-CP collision



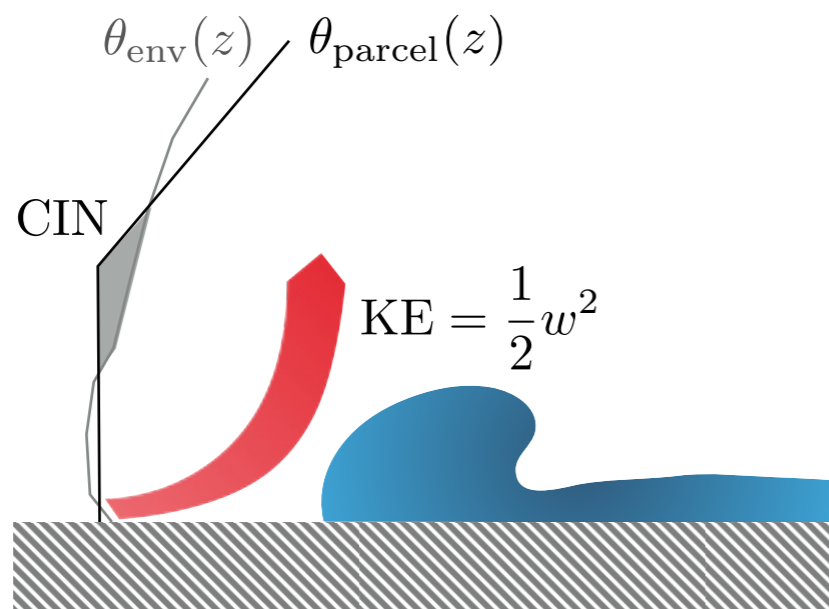
Vertical velocity - triple collision



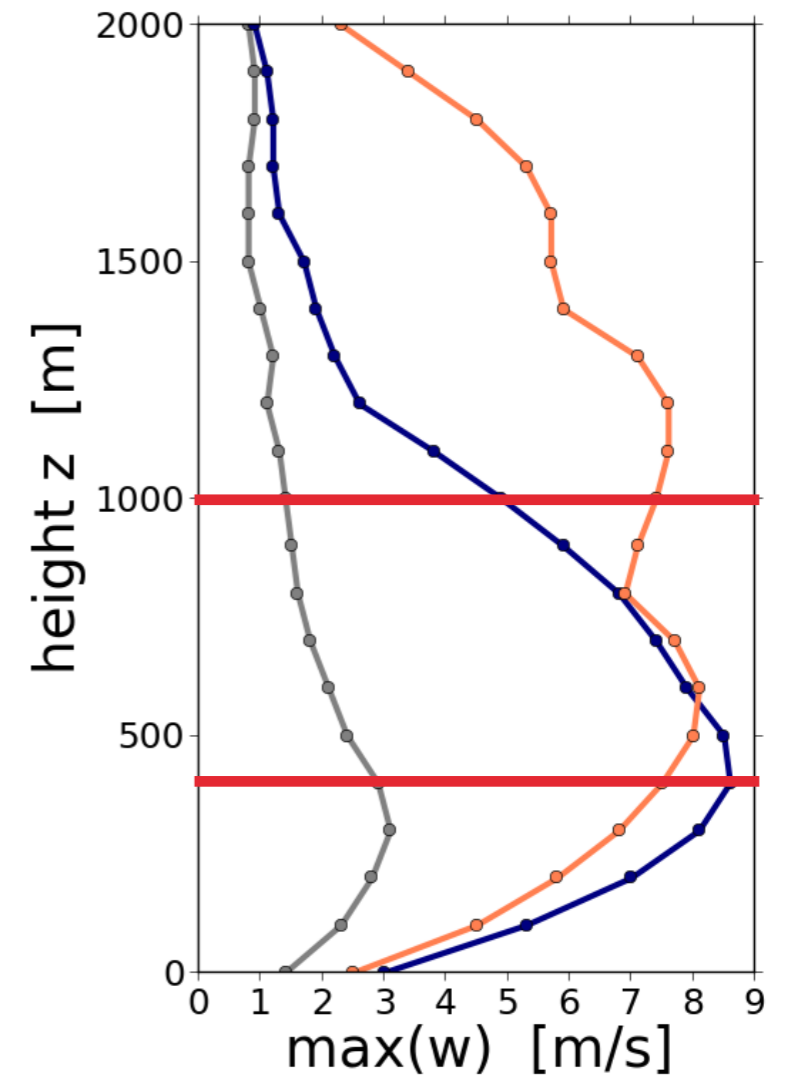
- single CP (undisturbed front)
- 2-CP collision
- 3-CP collision



Convection triggering



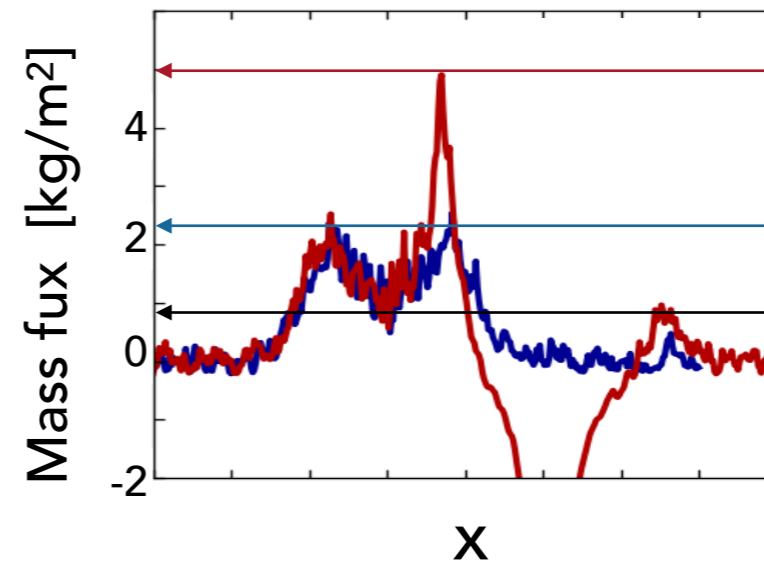
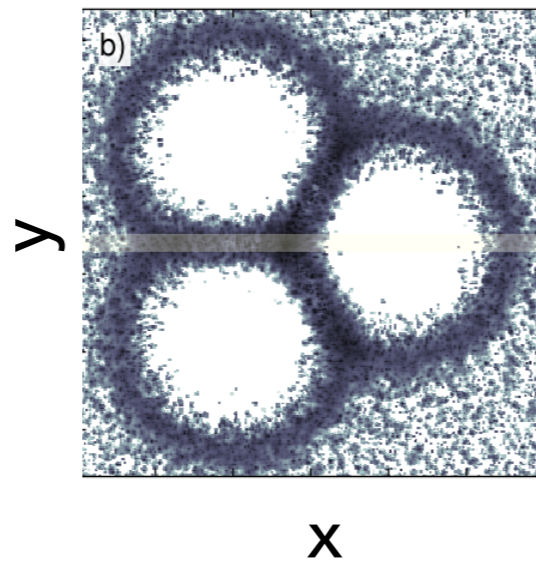
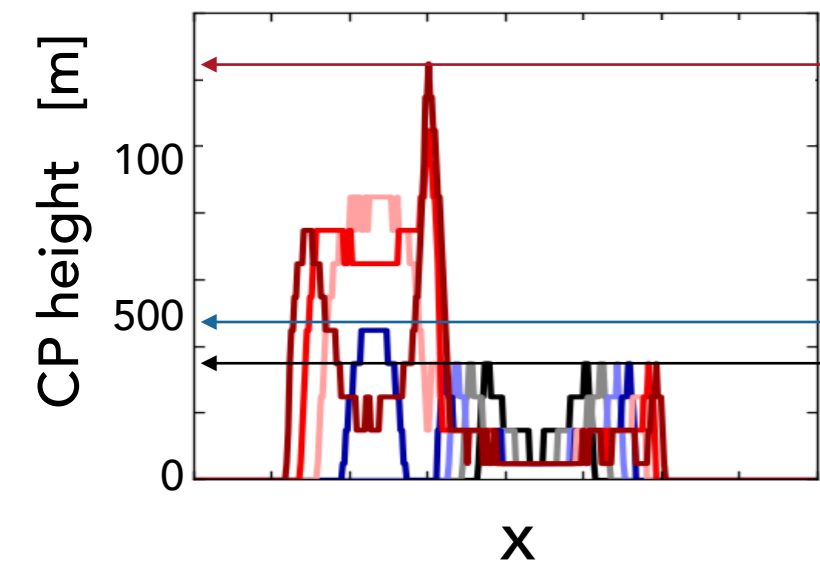
Triggering condition: $KE = \frac{1}{2}w^2 > |CIN|$



Vertical mass (moisture) flux & cold pool height

Cold pool height

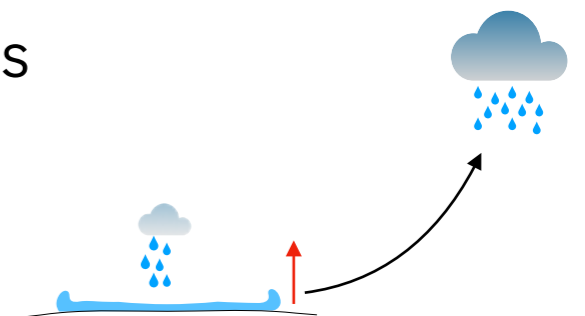
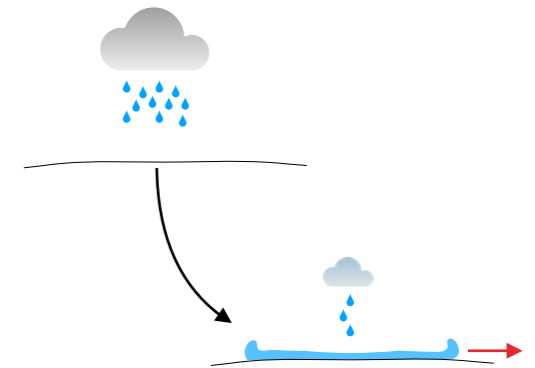
Vertical mass flux



- single CP
- 2-CP collision
- 3-CP collision

Conclusions

- **Convection triggering:**
 - Stronger updrafts in 2-CP collisions
 - > *strongly stratified / inhibited environments*
 - Deeper updrafts & highest mass flux in 3-CP collisions
 - > *pre-moistening in (deep) convection*
- **Climate Models:** need representation of cold pool collisions
 - > organisation of the cloud field
 - > precipitation intensity



Thank you for your input: bettina.meyer@nbi.ku.dk

